



LAMPIRAN

Lampiran 1

Menunjukkan turunan dari $f(H) = \pi_{ij}$ adalah $f'(H) = \pi_{ij}(1 - \pi_{ij})$:

Diketahui :

$$f(H) = \pi_{ij} = \pi(\mathbf{x}_{ij}) = \frac{e^{(\beta_0 + \beta_1 x_{1ij} + \dots + \beta_P x_{Pij})}}{1 + e^{(\beta_0 + \beta_1 x_{1ij} + \dots + \beta_P x_{Pij})}}$$

Maka turunan pertama dari $f'(H)$ adalah sebagai berikut :

$$\begin{aligned} f'(H) &= \frac{e^{(\beta_0 + \beta_1 x_{1ij} + \dots + \beta_P x_{Pij})} (1 + e^{(\beta_0 + \beta_1 x_{1ij} + \dots + \beta_P x_{Pij})}) - e^{(\beta_0 + \beta_1 x_{1ij} + \dots + \beta_P x_{Pij})} e^{(\beta_0 + \beta_1 x_{1ij} + \dots + \beta_P x_{Pij})}}{(1 + e^{(\beta_0 + \beta_1 x_{1ij} + \dots + \beta_P x_{Pij})})^2} \\ &= \frac{e^{(\beta_0 + \beta_1 x_{1ij} + \dots + \beta_P x_{Pij})} + (e^{(\beta_0 + \beta_1 x_{1ij} + \dots + \beta_P x_{Pij})})^2 - (e^{(\beta_0 + \beta_1 x_{1ij} + \dots + \beta_P x_{Pij})})^2}{(1 + e^{(\beta_0 + \beta_1 x_{1ij} + \dots + \beta_P x_{Pij})})^2} \\ &= \frac{e^{(\beta_0 + \beta_1 x_{1ij} + \dots + \beta_P x_{Pij})}}{(1 + e^{(\beta_0 + \beta_1 x_{1ij} + \dots + \beta_P x_{Pij})})^2} \\ &= \left(\frac{e^{(\beta_0 + \beta_1 x_{1ij} + \dots + \beta_P x_{Pij})}}{1 + e^{(\beta_0 + \beta_1 x_{1ij} + \dots + \beta_P x_{Pij})}} \right) \left(\frac{1}{1 + e^{(\beta_0 + \beta_1 x_{1ij} + \dots + \beta_P x_{Pij})}} \right) \\ &= \pi(\mathbf{x}_{ij})(1 - \pi(\mathbf{x}_{ij})) \end{aligned}$$

$\pi(\mathbf{x}_{ij})$ dapat dituliskan sebagai π_{ij} , sehingga $f'(H)$ pada persamaan di atas

dapat ditulis dalam bentuk :

$$f'(H) = \pi_{ij}(1 - \pi_{ij})$$

Lampiran 2

Data hasil survey mengenai penggunaan hak pilih dalam pemilu di Eropa.

	ctry_jdi(3300)	individual_jdi(3300)	tumout(3300)	age_at_elect(3300)	pcintr(3300)	partymember(3300)	minethnic(3300)	sex(3300)
1	1	1	1	46	0	0	0	0
2	1	2	1	48	0	0	0	1
3	1	3	1	37	1	0	0	1
4	1	4	0	30	1	0	0	1
5	1	5	1	50	1	0	0	1
6	1	6	1	66	0	0	0	0
7	1	7	1	68	1	0	0	0
8	1	8	1	40	0	0	1	1
9	1	9	1	49	1	0	1	1
10	1	10	1	56	1	0	0	0
11	1	11	1	44	0	0	0	1
12	1	12	0	77	0	0	0	0
13	1	13	1	73	1	0	0	0
14	1	14	0	75	1	0	0	1
15	1	15	1	33	1	0	0	0
16	1	16	1	43	1	0	0	1
17	1	17	1	37	0	0	0	1
18	1	18	1	58	1	1	0	0
19	1	19	1	53	1	0	0	1
20	1	20	1	74	1	0	0	0
21	1	21	1	38	1	0	0	1
22	1	22	1	36	1	0	0	1
23	1	23	1	74	1	1	0	0
24	1	24	1	54	0	0	0	1
25	1	25	0	76	0	0	0	1
26	1	26	1	37	0	0	0	1
27	1	27	1	50	1	0	0	1
28	1	28	1	34	0	0	0	1
29	1	29	1	30	0	1	0	0
30	1	30	1	39	0	0	0	0
31	1	31	1	20	1	1	0	0
32	1	32	0	26	1	1	0	0
33	1	33	1	30	0	0	0	1
34	1	34	0	38	0	0	0	1
35	1	35	0	63	0	0	0	1
36	1	36	0	42	0	0	0	0
37	1	37	1	31	1	0	0	0
38	1	38	1	62	1	1	0	0
39	1	39	1	33	1	0	0	0
40	1	40	0	76	1	0	0	0
41	1	41	1	80	0	0	0	1
42	1	42	1	24	1	0	0	0
43	1	43	0	60	0	0	1	1
44	1	44	0	38	0	0	0	1
45	1	45	1	27	1	1	0	0
46	1	46	1	60	1	0	0	1
47	1	47	1	36	0	0	0	1
48	1	48	0	36	1	0	0	1
49	1	49	1	36	0	0	0	1
50	1	50	1	37	0	1	0	1
51	1	51	1	66	1	1	0	0
52	1	52	1	51	1	1	0	0
53	1	53	1	44	1	0	0	1
54	1	54	0	24	0	0	0	0
55	1	55	1	37	1	1	0	0
56	1	56	1	43	1	0	0	1
57	1	57	1	52	0	1	1	0
58	1	58	1	64	0	0	0	0
59	1	59	1	46	0	0	0	1
60	1	60	1	78	0	0	0	1
61	1	61	1	47	1	1	0	0

	city_id(3300)	individual_id(330)	turnout(3300)	age_id_cledid(33)	polint(3300)	partymember(33)	minidinic(3300)	sex(33)
82	1	66	1	44	1	0	0	1
83	1	66	1	52	1	0	0	0
84	1	67	1	28	0	0	0	1
85	1	68	1	72	1	1	0	0
86	1	70	0	37	1	1	0	0
87	1	71	1	29	0	0	0	1
88	1	72	0	56	1	0	0	0
89	1	73	1	53	1	1	0	0
70	1	74	1	34	1	0	0	0
71	1	76	1	58	1	0	0	0
72	1	77	1	32	0	0	0	1
73	1	78	1	60	1	0	0	1
74	1	78	0	50	1	0	0	1
75	1	80	1	40	1	0	0	0
76	1	81	1	75	1	0	0	0
77	1	82	0	37	0	0	0	0
78	1	83	1	19	1	1	0	1
79	1	85	1	36	1	0	0	0
80	1	86	1	50	0	0	0	0
81	1	87	1	32	1	0	0	0
82	1	88	1	54	1	1	0	0
83	1	89	1	59	1	1	0	0
84	1	90	1	39	0	1	0	1
85	1	91	1	40	0	0	0	1
86	1	92	1	62	0	0	0	0
87	1	93	1	60	1	0	0	1
88	1	94	1	76	1	0	0	0
89	1	95	1	18	1	1	0	0
90	1	96	1	26	1	0	0	1
91	1	97	1	63	1	0	0	0
92	1	98	1	22	0	1	0	0
93	1	99	1	40	1	1	0	0
94	1	100	1	32	1	0	0	0
95	1	101	1	41	0	0	0	1
96	1	102	1	38	1	0	0	0
97	1	103	1	28	1	0	0	1
98	1	104	1	58	1	0	0	1
99	1	105	1	45	0	0	0	1
100	1	106	1	49	0	0	0	1
101	1	107	1	32	0	0	0	0
102	1	108	1	84	1	1	0	1
103	1	109	1	59	0	0	0	1
104	1	110	1	27	1	0	0	1
105	1	111	1	55	1	0	0	1
106	1	112	0	50	0	0	0	1
107	1	113	0	33	0	0	0	0
108	1	114	0	20	0	0	0	0
109	1	115	1	29	1	0	0	1
110	1	116	0	21	0	0	0	1
111	1	117	1	30	1	0	0	1
112	1	118	0	50	1	0	0	1
113	1	119	1	35	1	0	0	1
114	1	120	1	38	0	0	0	1
115	1	122	1	20	0	0	0	1
116	1	123	0	48	0	0	0	0
117	1	125	0	51	0	0	0	0
118	1	126	0	50	0	0	0	0
119	1	127	1	29	1	0	0	0
120	1	128	0	52	0	0	0	0
121	1	129	1	52	1	0	0	0
122	1	130	0	32	0	0	0	1
123	1	131	1	41	1	0	0	0
124	1	132	1	37	1	0	0	1
125	1	133	0	58	1	0	0	1
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	ctry	id(3300)	Individual	id(3300)	turnout(3300)	age	at	elect(3300)	polintr(3300)	partymember(3300)	minethnic(3300)	sex(3300)
179	1	180	100	0	41	1	0	1	0	1	0	
180	1	181	189	1	83	0	0	0	0	0	1	
181	1	182	190	1	38	1	0	0	0	0	0	
182	1	183	191	1	48	1	0	0	0	0	1	
183	1	184	192	1	77	0	0	0	0	0	1	
184	1	185	193	1	41	1	0	1	0	1	0	
185	1	186	194	1	33	1	0	1	0	0	1	
186	1	187	195	1	37	1	0	0	0	0	1	
187	1	188	196	1	27	1	0	0	0	0	1	
188	1	189	197	0	39	0	0	0	0	0	1	
189	1	190	198	1	34	1	0	0	0	0	1	
190	1	191	199	1	30	0	0	0	0	0	1	
191	1	192	200	1	61	1	1	0	0	0	0	
192	2	193	201	1	53	1	0	0	0	0	1	
193	2	194	202	1	30	0	0	0	0	0	1	
194	2	195	203	1	34	1	0	0	0	0	0	
195	2	196	204	1	41	0	0	0	0	0	1	
196	2	197	205	1	42	1	0	0	0	0	1	
197	2	198	206	1	54	1	0	0	0	0	0	
198	2	199	207	1	71	1	0	0	0	0	0	
199	2	200	208	1	33	0	0	0	0	0	0	
200	2	201	209	1	52	1	0	0	0	0	0	
201	2	202	210	1	10	0	0	0	0	0	0	
202	2	203	211	0	70	0	0	0	0	0	0	
203	2	204	212	0	36	0	0	0	0	0	1	
204	2	205	213	1	44	1	0	0	0	0	0	
205	2	206	214	1	40	1	0	0	0	0	0	
206	2	207	215	1	60	0	0	0	0	0	1	
207	2	208	217	1	42	0	0	0	0	0	1	
208	2	209	218	1	44	1	0	0	0	0	0	
209	2	210	219	1	76	1	0	0	0	0	0	
210	2	211	221	1	64	0	0	0	0	0	1	
211	2	212	222	1	73	1	1	0	0	0	1	
212	2	213	223	1	77	1	1	0	0	0	1	
213	2	214	224	1	52	1	0	0	0	0	1	
214	2	215	225	0	88	0	0	0	0	0	1	
215	2	216	226	0	85	0	0	0	0	0	0	
216	2	217	227	1	50	0	1	0	0	0	0	
217	2	218	228	1	57	1	0	0	0	0	1	
218	2	219	229	1	28	1	0	0	0	0	0	
219	2	220	230	1	27	0	0	0	0	0	1	
220	2	221	231	1	64	0	0	0	0	0	1	
221	2	222	232	0	29	0	0	0	0	0	1	
222	2	223	233	1	55	0	0	0	0	0	0	
223	2	224	234	1	84	1	0	0	0	0	1	
224	2	225	235	1	70	1	0	0	0	0	0	
225	2	226	236	1	11	0	0	0	0	0	0	
226	2	227	237	1	22	0	0	0	0	0	1	
227	2	228	238	1	70	0	0	0	0	0	1	
228	2	229	239	1	27	1	0	0	0	0	0	
229	2	230	240	1	70	0	0	0	0	0	0	
230	2	231	241	1	21	0	0	0	0	0	1	
231	2	232	242	1	39	0	0	0	0	0	0	
232	2	233	243	1	40	1	0	0	0	0	0	
233	2	234	244	1	45	1	0	0	0	0	0	
234	2	235	245	1	20	0	0	0	0	0	1	
235	2	236	246	1	55	1	1	0	0	0	0	
236	2	237	247	1	40	1	0	0	0	0	0	
237	2	238	248	1	43	0	0	0	0	0	0	
238	2	239	249	0	31	0	0	0	0	0	1	
239	2	240	250	1	27	1	0	0	0	0	0	
240	2	241	251	1	56	1	0	0	0	0	0	
241	2	242	252	1	43	1	0	0	0	0	1	
242	2	243	253	1	27	1	0	0	0	0	0	
:	:	:	:	:	:	:	:	:	:	:	:	

	ctry_id(3300)	individual_id(330)	turnout(3300)	age_at_elect(33)	politic(3300)	partymember(33)	minelimit(3300)	sex(33)
320	2	331	1	48	1	0	0	1
321	2	332	1	56	0	0	0	1
322	2	333	1	26	0	0	0	1
323	2	334	1	30	0	0	0	0
324	2	335	1	74	0	0	0	0
325	2	336	1	51	0	0	0	1
326	2	337	1	30	0	0	0	1
327	2	338	1	46	1	0	0	0
328	2	339	1	54	1	0	0	1
329	2	340	0	19	0	0	0	0
330	4	341	1	20	0	0	0	0
331	4	342	1	43	0	0	0	0
332	4	343	1	43	0	0	0	0
333	4	344	1	67	0	0	0	1
334	4	345	1	61	1	0	0	0
335	4	346	1	54	0	0	0	1
336	4	347	0	57	0	0	0	1
337	4	348	0	64	0	0	0	1
338	4	349	1	68	0	0	0	1
339	4	350	0	36	0	0	0	1
340	4	351	0	36	0	0	0	0
341	4	352	1	36	0	0	0	1
342	4	353	1	69	1	0	0	1
343	4	354	0	31	0	0	0	1
344	4	355	1	60	1	0	0	1
345	4	356	1	42	1	0	0	1
346	4	357	1	82	1	0	0	1
347	4	358	1	49	1	0	0	0
348	4	359	1	72	1	0	0	0
349	4	360	1	60	0	0	0	1
350	4	361	0	54	0	0	0	0
351	4	362	1	45	0	0	1	1
352	4	363	1	23	1	0	0	0
353	4	364	0	32	0	0	0	0
354	4	365	0	85	0	0	0	1
355	4	366	1	54	0	0	0	0
356	4	367	1	56	0	0	0	1
357	4	368	1	74	0	0	0	1
358	4	369	1	21	0	0	0	1
359	4	370	1	73	0	0	0	1
360	4	371	0	80	0	0	0	1
361	4	372	1	77	0	0	0	1
362	4	373	1	56	0	0	0	0
363	4	374	0	58	1	0	0	0
364	4	375	0	31	0	0	0	1
365	4	376	0	71	0	0	0	0
366	4	377	0	75	0	0	0	0
367	4	378	1	58	1	0	0	0
368	4	379	0	59	0	0	0	0
369	4	380	1	19	0	0	0	0
370	4	381	0	50	0	0	0	0
371	4	382	1	61	1	0	0	1
372	4	383	0	45	0	0	1	0
373	4	384	0	40	0	0	0	0
374	4	385	1	80	0	0	0	1
375	4	386	1	85	0	0	0	0
376	4	387	1	42	1	0	0	1
377	4	388	0	21	0	0	0	1
378	4	389	1	66	1	0	0	0
379	4	390	1	64	0	0	0	0
380	4	391	1	39	1	1	0	1
381	4	392	0	45	0	1	0	0
382	4	393	1	30	0	0	0	1
383	4	394	1	78	0	1	0	1
:	:	:	:	:	:	:	:	:

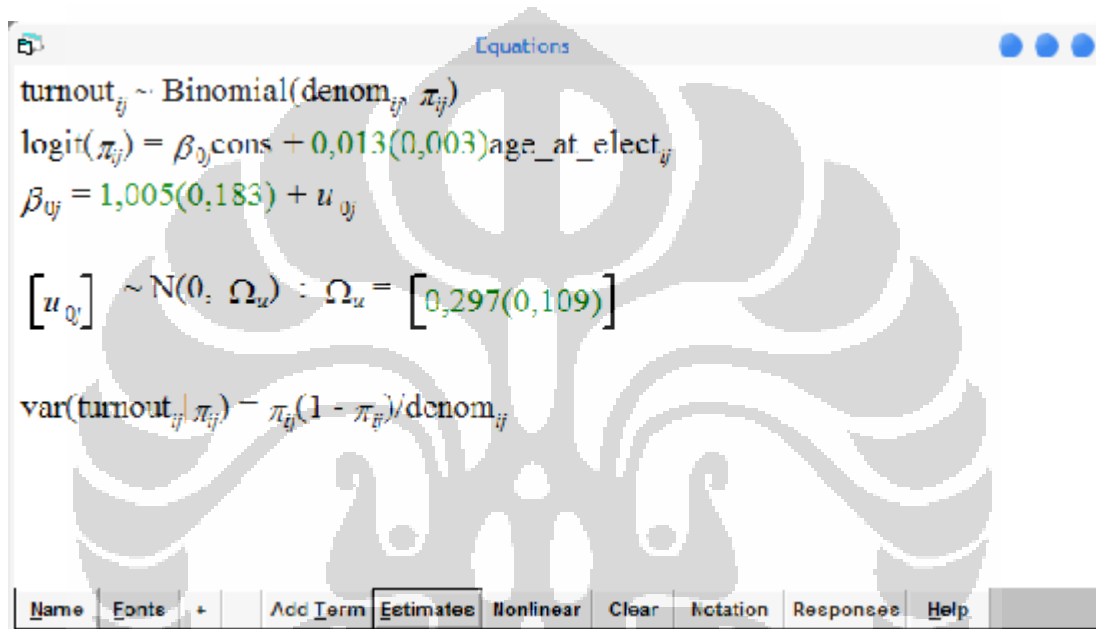
ctry	id(3300)	individual	id(330)	turnout(3300)	age	at	elect(33)	polintr(3300)	partymember(33)	minethnic(3300)	sex(3:
3153	21	3213	1	1	45		0	0	0	0	1
3154	21	3214	1	1	38		0	0	0	0	0
3155	21	3215	0	0	58		1	0	0	0	0
3156	21	3216	1	1	63		1	0	0	0	1
3157	21	3217	0	0	47		0	0	0	0	0
3158	21	3218	1	1	57		1	0	0	0	1
3159	21	3219	1	1	43		0	0	0	0	0
3160	21	3220	1	1	27		1	0	0	0	0
3181	21	3222	0	0	22		1	0	0	0	1
3182	21	3223	1	1	32		0	0	0	0	0
3163	21	3224	1	1	36		1	0	0	0	0
3164	22	3225	1	1	28		0	0	0	0	0
3165	22	3226	1	1	43		0	0	0	0	1
3166	22	3227	1	1	77		1	0	0	0	0
3167	22	3228	1	1	40		1	0	0	0	1
3188	22	3230	1	1	30		0	0	0	0	0
3189	22	3231	1	1	39		1	0	0	0	0
3170	22	3232	1	1	80		0	0	0	0	1
3171	22	3233	0	0	25		0	0	0	0	1
3172	22	3234	0	0	47		0	0	0	0	1
3173	22	3235	1	1	41		1	0	0	0	0
3174	22	3236	1	1	75		0	0	0	0	0
3175	22	3237	1	1	43		1	0	0	0	0
3176	22	3238	1	1	43		0	0	0	0	1
3177	22	3239	1	1	21		1	0	0	0	0
3178	22	3240	0	0	42		0	0	0	0	1
3179	22	3241	0	0	45		0	0	0	0	1
3180	22	3242	1	1	79		1	0	0	0	1
3181	22	3243	1	1	52		0	0	0	0	1
3182	22	3244	1	1	72		1	0	0	0	1
3183	22	3245	1	1	34		0	0	0	0	1
3184	22	3246	0	0	25		0	0	0	0	1
3185	22	3247	1	1	81		1	1	0	0	0
3186	22	3248	1	1	35		0	0	0	0	0
3187	22	3249	0	0	19		0	0	0	0	1
3188	22	3250	1	1	39		1	1	0	0	0
3189	22	3251	1	1	44		0	0	0	0	1
3190	22	3252	1	1	54		1	1	0	0	0
3191	22	3253	1	1	45		0	0	0	0	1
3192	22	3254	0	0	70		0	0	0	0	0
3193	22	3255	1	1	50		0	0	0	0	0
3194	22	3256	1	1	27		0	0	0	0	1
3195	22	3257	1	1	38		1	1	0	0	0
3196	22	3258	1	1	76		0	0	0	0	1
3197	22	3259	1	1	70		0	0	0	0	1
3198	22	3260	1	1	55		0	0	0	0	1
3199	22	3261	1	1	40		0	0	0	0	1
3200	22	3262	0	0	39		0	0	0	0	1
3201	22	3263	1	1	75		1	0	0	0	1
3202	22	3264	1	1	44		0	0	0	0	1
3203	22	3265	1	1	40		1	0	0	0	0
3204	22	3266	1	1	38		1	0	0	0	0
3205	22	3267	0	0	20		0	0	0	0	0
3206	22	3268	1	1	35		1	1	0	0	0
3207	22	3269	1	1	73		1	0	0	0	1
3208	22	3270	1	1	70		1	0	0	0	1
3209	22	3271	1	1	52		1	0	0	0	1
3210	22	3272	0	0	70		0	0	0	0	1
3211	22	3273	1	1	30		0	0	0	0	1
3212	22	3274	1	1	61		0	0	0	0	1
3213	22	3275	1	1	42		0	0	0	0	1
3214	22	3276	1	1	87		0	0	0	0	0
3215	22	3277	1	1	24		0	0	0	0	0
3216	22	3278	1	1	73		1	0	0	0	0
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	ctry_id(J300)	individual_id(J3)	turnout(J300)	age_at_elect(J)	pointnr(J300)	partymember(J)	minethnc(J300)	sex(J)
3269	22	3331	0	23	0	0	1	0
3270	22	3332	1	51	1	0	0	0
3271	22	3333	1	59	1	0	0	1
3272	22	3334	1	53	0	0	0	0
3273	22	3335	1	62	0	0	0	0
3274	22	3336	1	44	1	0	0	1
3275	22	3337	1	27	1	0	0	0
3276	22	3338	0	22	1	0	0	1
3277	22	3339	1	36	0	0	0	1
3278	22	3340	1	55	1	0	0	0
3279	22	3341	1	61	1	0	0	1
3280	22	3342	1	67	1	0	0	0
3281	22	3343	1	37	0	0	0	1
3282	22	3344	0	51	0	0	0	1
3283	22	3345	1	78	1	0	0	1
3284	22	3346	1	61	1	0	0	1
3285	22	3347	1	50	1	0	0	0
3286	22	3348	1	45	1	1	0	0
3287	22	3349	1	39	0	0	0	1
3288	22	3350	1	32	0	0	0	0
3289	22	3351	1	32	0	0	0	0
3290	22	3352	0	19	0	0	0	1
3291	22	3353	1	49	1	0	0	0
3292	22	3354	1	26	0	0	0	1
3293	22	3355	0	24	0	0	0	1
3294	22	3356	0	35	0	0	0	0
3295	22	3357	1	32	0	0	0	0
3296	22	3358	1	48	1	0	0	0
3297	22	3359	1	23	0	0	0	0
3298	22	3360	1	31	1	0	0	0
3299	22	3361	1	26	0	0	0	1
3300	22	3362	0	22	0	0	0	0

Lampiran 3

Output MlwiN untuk analisis data hasil survey mengenai penggunaan hak pilih dalam pemilu di Eropa.

Untuk model regresi logistik 2-Level dengan satu variabel penjelas :



The screenshot shows the MlwiN Equations window with the following model specifications:

$$\text{turnout}_{ij} \sim \text{Binomial}(\text{denom}_{ij}, \pi_{ij})$$

$$\text{logit}(\pi_{ij}) = \beta_{0j} \text{cons} + 0,013(0,003) \text{age_at_elect}_{ij}$$

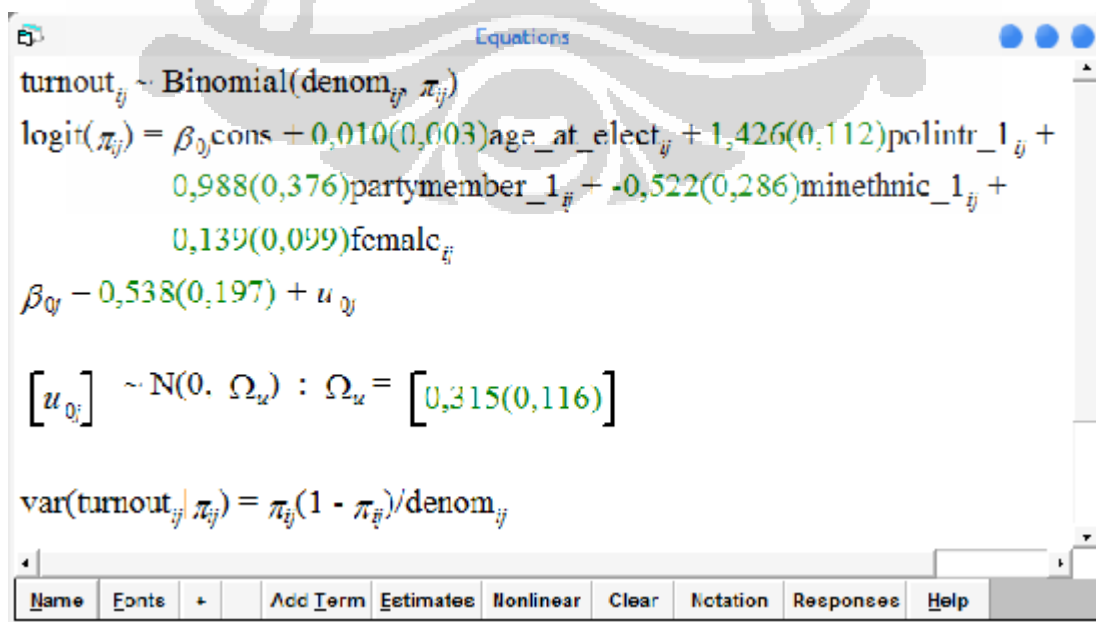
$$\beta_{0j} = 1,005(0,183) + u_{0j}$$

$$[u_{0j}] \sim N(0, \Omega_u) : \Omega_u = [0,297(0,109)]$$

$$\text{var}(\text{turnout}_{ij} | \pi_{ij}) = \pi_{ij}(1 - \pi_{ij}) / \text{denom}_{ij}$$

The interface includes a toolbar with buttons for Name, Fonts, Add Term, Estimatee, Nonlinear, Clear, Notation, Responses, and Help.

Untuk model regresi logistik 2-Level dengan lima variabel penjelas :



The screenshot shows the MlwiN Equations window with the following model specifications:

$$\text{turnout}_{ij} \sim \text{Binomial}(\text{denom}_{ij}, \pi_{ij})$$

$$\text{logit}(\pi_{ij}) = \beta_{0j} \text{cons} + 0,010(0,003) \text{age_at_elect}_{ij} + 1,426(0,112) \text{polintr_1}_{ij} + 0,988(0,376) \text{partymember_1}_{ij} + -0,522(0,286) \text{minethnic_1}_{ij} + 0,139(0,099) \text{fcmalc}_{ij}$$

$$\beta_{0j} = 0,538(0,197) + u_{0j}$$

$$[u_{0j}] \sim N(0, \Omega_u) : \Omega_u = [0,315(0,116)]$$

$$\text{var}(\text{turnout}_{ij} | \pi_{ij}) = \pi_{ij}(1 - \pi_{ij}) / \text{denom}_{ij}$$

The interface includes a toolbar with buttons for Name, Fonts, Add Term, Estimatee, Nonlinear, Clear, Notation, Responses, and Help.