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Simulasi Crossdock menggunakan software Arena

TESIS

Diajukan sebagai salah satu syarat untuk memperoleh gelar Magister Teknik

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FAKULTAS TEKNIK

PROGRAM STUDI TEKNIK INDUSTRI

DEPOK

JULI 2011

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Telah berhasil dipertahankan dihadapan Dewan Penguji dan diterima sebagai bagian persyaratan yang diperlukan untuk memperoleh gelar Master 2 Université d'Artois (Perancis) dan Magister Teknik pada Program Studi Teknik Industri, Fakultas Teknik, Universitas Indonesia

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Bethune-France, 22 Juni 2011

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ABSTRAK

Nama : Faizal
Program Studi : Teknik Industri
Judul : Simulasi Crossdock menggunakan software Arena Versi 13.5

Crossdock adalah salah satu teknik logistik baru di dalam penanganan material yang mana produk yang datang di pintu inbound langsung di muat di pintu outbound dimana tidak ada penyimpanan walaupun ada kurang dari satu hari bahkan kurang dari satu jam sehingga bisa menurunkan biaya inventori. Keuntungan yang terlihat jelas dari sistem crossdock adalah menurunkan dua komponen biaya yaitu penyimpanan dan pengambilan barang dari rak. Di dalam sistem crossdock barang datang dari beberapa pemasok di konsolidasikan di crossdock kemudian di distribusikan ke pelanggan. Skenario didalam model crossdock menggunakan simulasi Arena ini adalah terdapat tiga pintu inbound dan tiga pintu outbound dengan rata-rata waktu antar kedatangan satu truk per jam dengan waktu rata-rata pelayanan satu truck per jam. Model di jalankan selama dua belas jam dengan tiga puluh replikasi untuk mendapatkan tingkat kepercayaan > 95 %. Dan hasilnya adalah rata-rata kedatangan truk inbound adalah dua belas dengan tingkat kepercayaan 91 % sementara rata-rata truk yang keluar adalah sebelas dengan tingkat kepercayaan 90 %. Adapun untuk rata-rata tingkat kegunaan pintu inbound adalah 34.4% untuk pintu inbound satu, 30.3 % untuk pintu inbound dua dan 36.8% untuk pintu tiga. Sementara tingkat kegunaan dari forklift adalah 27.5 % untuk forklift satu, 17.8% untuk forklift dua, 19.6% untuk forklift tiga, 13.9% forklift empat, 13.7% untuk forklift lima, and 15.7% untuk forklift enam. Dan untuk waktu rata-rata pemindahan pallet adalah 1.13 menit untuk pallet satu, 1.19 menit untuk pallet 2 dan 1 menit untuk pallet tiga. Dari hasil simulasi diatas dapat disimpulkan bahwa sistem operasi crossdock harus dia rencanakan agar bisa mengoptmalkan penggunaan sumber daya yang di miliki.

Kata Kunci: crossdock, simulasi

ABSTRACT

Name : Faizal
Study Program : Industrial Engineering
Title : Crossdock Simulation with Arena

Crossdock is a new logistics technic in material handling which products directly shipments from inbound trucks to outbound trucks. Crossdock can reduce the cost of inventory with direct delivery product without storing. Some obvious advantages from crossdock First crossdock eliminates two cost- and labor-intensive functions: storage and order picking of a traditional warehouse, while still allowing it to serve receiving and shipping functions. The different between traditional warehouse and crossdock is in crossdock they eliminate storing activity, that's mean product came from plusieurs supplier consolidated inside crossdock and delivery directly to their destination. From our model we have three inbound door and three outbound door while inside the dock we have six forklift to transfer product from inbound door to outbound door. The interraival truck is EXPO (60) minutes and service time in this case time to discharge and load pallet from inbound dock and to outbound dock TRIA (30, 60, 90). Arena simulation is one of the discrete event simulation with the objective is mesure average waiting line of the queue, these mesure change only when entity enters and leaves the system. Our simulation run seven hundred twenty minutes with thirty replication and the result is average truck inbound enter the system 12 with halfwidth 9% and truck out 11 with halfwidth 10%. The average utilization inbound docks is 34.4%, 30.3 % and 36.8%. utilization of forklfit 27.5% for foklift 1, 17.8% for forklift 2, 19.6% for forklift 3, 13.9% forklift 4, 13.7% forklift 5, and 15.7% forklift 6. From the view of simulation we can conclue that The crossdock operation is need to be planned for to optimizing our resources utilization.

Keyword: crossdock, simulation



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Chapter. 1 Introduction

The Internship is an integral part of the master in Industrial Engineering Program in Faculte Science Applique (FSA) Universite Artois . This work term should make us valuable insight into professional and industry-oriented side of logistics in practice. To fulfill the academic requirements of the internship we are required to submit an internship report as well as presentation. And our subject is Cross dock with Arena Simulation

Started at 04 April 2011 until 04 July 2011 we have to working 08h per day , 5 day / weeks in Laboratoire Genie Informatique et Automatique de l'Artois (LGI2A).

Purpose of this study was to find out how crossdock operational working from view of simulation and then how to input it in Simulation Arena version 13.5.

1.1 Report Scheme

Chapter 1 . Introduction

In this chapter we describe about our program as a master 2 pro that at semester 2 in the second year we have to do internship about three month. In this chapter too we describe our reseach goal

Chapter 2. Literature review

In this chapter we describe what is crossdock. In order to gain a deep understanding on crossdock we make two question What is Crossdock and Why Crossdock. In this chapter we also do literature study of what is simulation, systems, modeling and discrete event simulation. And we also try to explore what is advantages or strengths of the Arena software version 13.5.

Chapter 3. Model Approach and Assumption

In this chapter we describe how the process flow of our model in order to make more easier in building our model after. And in this chapter we also provides information on the assumption that we use in our model. For example, inter arrival time trucks, number of pallet will discharge, length of our croosdock facility and speed of our forklift.

Chapter 4. the results and analysis

In this chapter we analyze the results of the model that we have made. To get an optimal performace for example minimum total waiting time in the product Inbound and outbound door door we use "Optquest for Arena"

Chapter 5. Conclusion

In this chapter we conclude about the utility of this simulation for various industrial fields.

Chapter 6. Reference and Appendix

1.2. Research Methodology

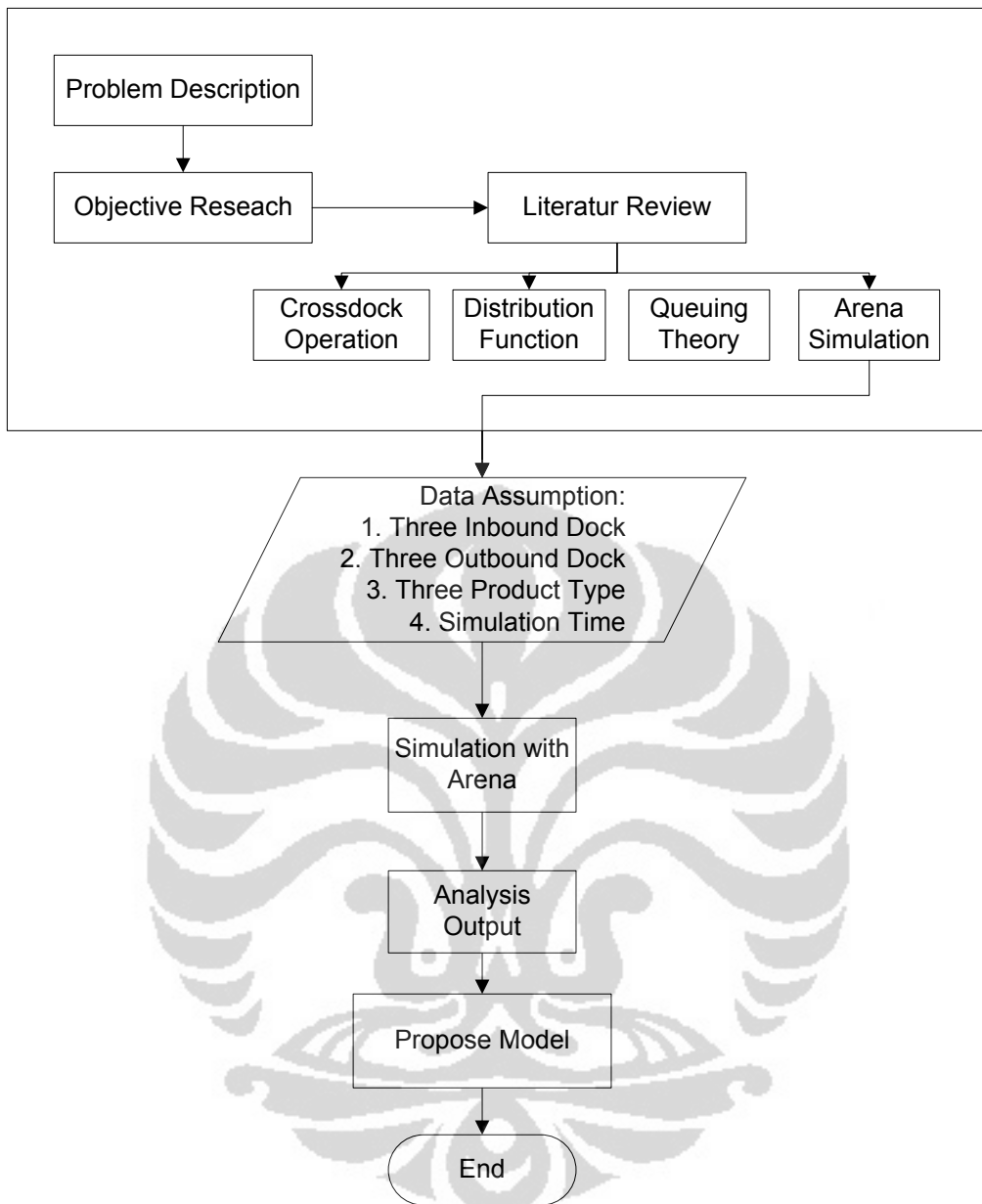


Figure 1.2.1 Research Methodology

Chapter. 2 Literatur Review

2.1 Cross dock as part of the logistics

Entering the competitive market nowadays makes the logistics industry seeking strategy to eliminate non value added activity to reduce cost and increase profit. As a consequence costs must be lowered throughout the chain by driving out unnecessary costs and focusing attention on adding value (Haag, S *et.al*, 2006)². Keah Choon Tan, (2000) in his framework of supply chain management said the objective in supply chain management and logistics is to reduced cycle time , inventory and increase customer satisfaction with providing visibility and consolidating distribution centers. Where warehouses is including inside (Tayful Altiok, benjamin melamed, 2007).

Warehouses are an essential component of any supply chain (Jinxiang Gu *et al.* 2007). Because it plays a very important role in all transfers of products from the place of origin to ultimate users (Danuta Kisperska-Moron, 1999). Traditional warehouse activities includes receiving, storage, order picking, and shipping. From the whole activities order picking is the most labour-intensive operation in warehouses as almost 55 % of the total warehouse operating expense and the second is storage 20%, receiving 15%, and the rest is shipping operation (Vijay Sangam, 2010, Rene de koster *et.al*, 2006). Crossdocking have a chance to cut almost a half of activity in traditional warehouse.

Crossdock is a new logistics technic in material handling which products directly shipments from inbound trucks to outbound trucks. In the other word Crossdock is optimization in warehousing system. Crossdock can reduce the cost of inventory with direct delivery without storing. The objective of daily cross-dock's operation plan is to assign the incoming trailers to the inbound door positions and the outgoing trailers to the outbound doors position, in order to minimise handling i.e., the total distance travelled by the freight itself or by the forklifts. (yuval cohen and baruch keren, 2009).

Crossdocking has some obvious advantages. First crossdocking eliminates two cost- and labor-intensive functions: storage and order picking of a traditional warehouse, while still allowing it to serve receiving and shipping functions (Zhengping Li *et.al*, 2007). Handling costs is reduced because it minimizes "the number of touches". Second, the speed of material movement is faster, cargo normally takes a few days and even months in traditional ware- housing and it only normally takes less than 24 hours in a crossdock. Third, inventory is much lower and the throughput is higher in crossdocking compared to traditional warehousing. In addition, when timing is well coordinated,

products can be made available in shorter time windows, thus reducing cycle times. So crossdocking's impact to supply chain is to make it more responsive to customer demand as compared to traditional warehousing.

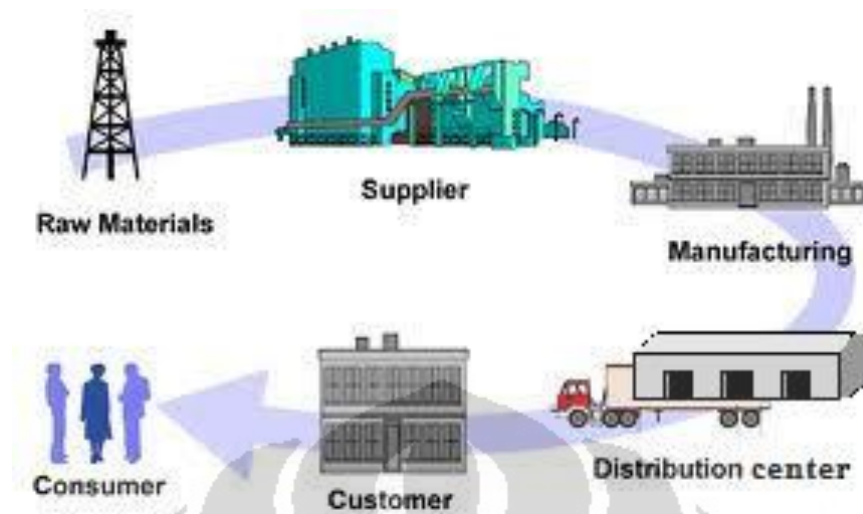


Figure 2.1 Cross dock in Supply Chain System

2.2 The Advantage of Cross dock

(Yan Liu, Soemon Takakuwa 2010) The primary objective of crossdocking is to **eliminate storage**, excessive handling, and lead time while minimizing transportation and storage costs and maintaining a high level of customer service.

Crossdocking's impact to supply chain is to make it more **responsive** to customer demand (Zhengping Li *et.al* 2007). Crossdocking has some obvious advantages. First crossdocking eliminates two cost- and labor-intensive functions: storage and order picking of a traditional warehouse, while still allowing it to serve receiving and shipping functions. Second, the speed of material movement is faster because products arrive in Inbound dock has their destination. Third, inventory is much lower and the throughput is higher in crossdocking compared to traditional warehousing. In addition, when timing is well coordinated, products can be made available in shorter time windows, thus reducing cycle times.

Gue and Kang 2001, Crossdock is a way to **reduce inventory holding cost** and transportation cost.

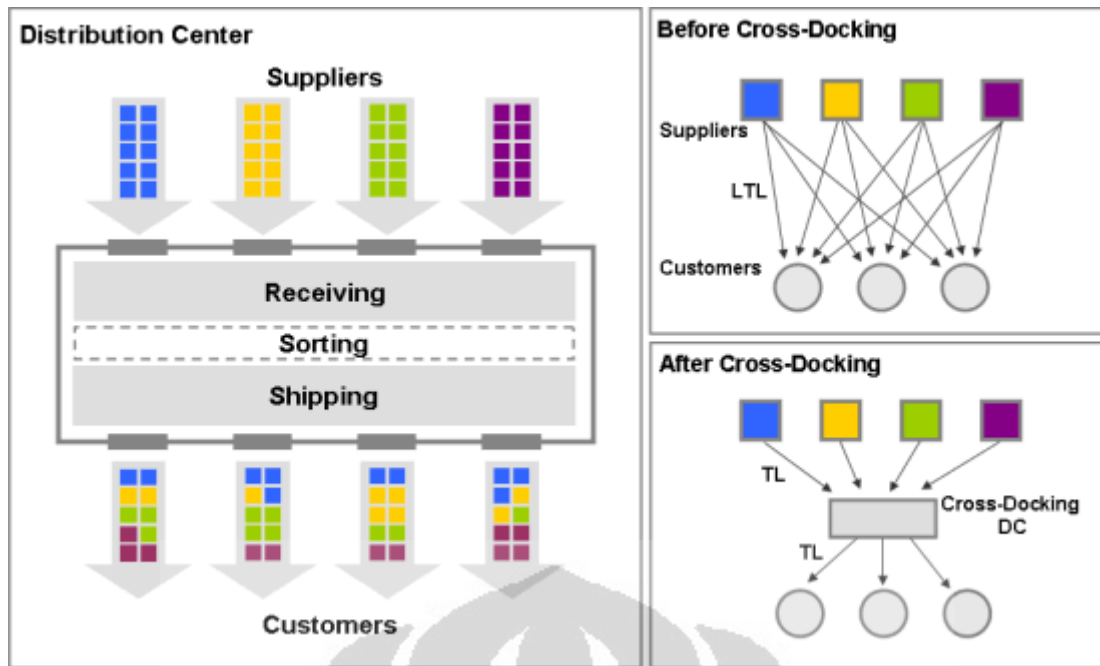


Figure 2.2 Distribution before and after Crossdock

2.4 Queuing Theory

The objective of queuing analysis is to offer reasonably satisfactory service to waiting customers (hamdi taha 2007) which can then used to design the service installation and minimize cost due to waiting time and increase service facility. the point important from the queuing theory is the Poisson and Exponential, because it helps identify the situation where queuing applied in our situation.

The poisson process have been used to model external arrivals to a variety systems, where arriving entity make “ independent arrival decisions.” For example truck arrive is not “ coordinated “ with discharge pallet in Inbound door, and truck arrivals are usually independent of each other (tayfur altiok 2007). Meaning we cannot predict when truck will arrive. The poisson pdf is defined as

$$P\{x = k\} = \frac{\lambda^k e^{-\lambda}}{k!}, k = 0, 1, 2, \dots$$

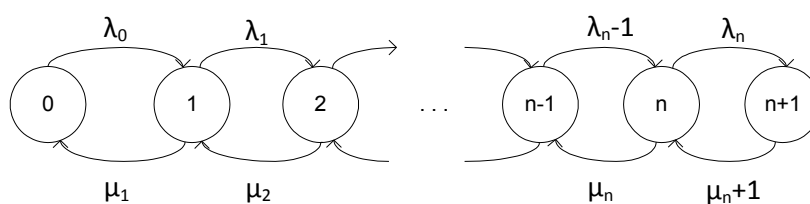


Figure 2.4.1 Poisson queues transition diagram

Where

λ = Average arrival rate
 μ = Average service time

There are three components in the system queue is :

1. The Arrival of the population to be served
2. Queues
3. Service facilities

The arrival of entity is represented the interarrival time and the service describe by the service time per entity.

The queue discipline, which represent the order in which entity are selected from queue, is important factor in the analysis of queuing models. The following table is given in queuing system characteristic

Queue characteristic	Symbol	meaning
Interarrival time or service time	D	Deterministic
	M	Exponential
	Oak	Erlang distribution
	G	Other distribution
Queuing Dicipline	FIFO	First In First Out
	LIFO	Last in First Out
	Siro	Service in Random Order
	PRI	The Order of Priority

Table 2.4.1 Queuing System Characteristic

2.4.1 Multiple Server Model

in our model, there are c parallel servers. The Arrival rate is λ and the service rate per server is μ .

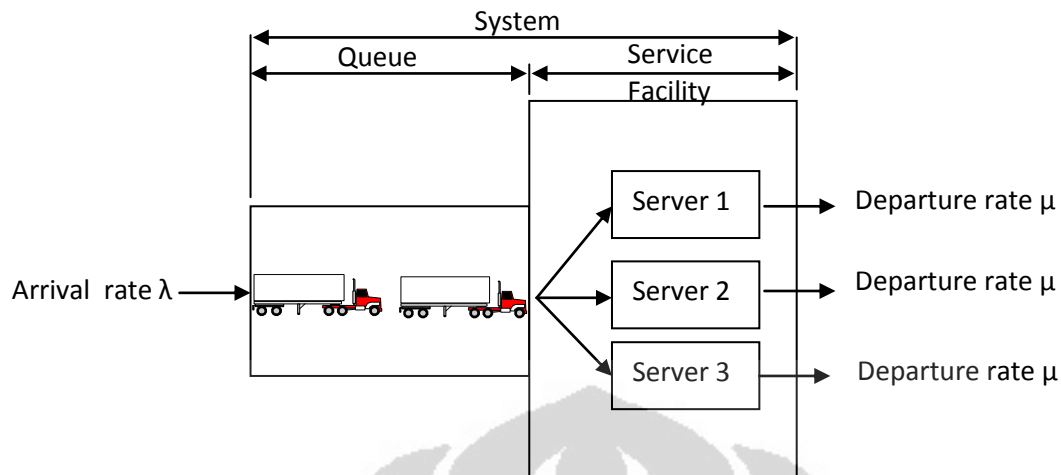


Figure 2.4.2 Schematic of a queuing system with single queue parallel servers M/M/c

The effect of using c (server) parallel is proportionate increase in the facility service rate. The arrival rate is λ and the service rate is μ . Because there is no limit on the number in the system, $\lambda_{\text{eff}} = \lambda$. Are thus defined

$$\lambda_n = \lambda, n \geq 0$$

$$\mu_n = \begin{cases} n\mu, & n < c \\ c\mu, & n \geq c \end{cases}$$

Thus,

$$\rho_n = \begin{cases} \frac{\lambda^n}{\mu(2\mu)(3\mu)\dots(n\mu)} \rho_0 = \frac{\lambda^n}{n! \mu^n} \rho_0 = \frac{\rho^n}{n!} \rho_0, & n < c \\ \frac{\lambda^n}{\left(\prod_{i=1}^c i\mu\right)(c\mu)^{n-c}} \rho_0 = \frac{\lambda^n}{c! c^{n-c} \mu^n} \rho_0 = \frac{\rho^n}{c! c^{n-c}} \rho_0, & n \geq c \end{cases}$$

Letting $\rho = \frac{\lambda}{\mu}$, and assuming $\frac{\rho}{c} < 1$, the value of ρ_0 is determined from $\sum_{n=0}^{\infty} \rho_n = 1$

Which gives,

$$\rho_0 = \left\{ \sum_{n=0}^{c-1} \frac{\rho^n}{n!} + \frac{\rho^c}{c!} \sum_{n=c}^{\infty} \left(\frac{\rho}{c} \right)^{n-c} \right\}^{-1}$$

$$= \left\{ \sum_{n=0}^{c-1} \frac{\rho^n}{n!} + \frac{\rho^c}{c!} \left(\frac{1}{1 - \frac{\rho}{c}} \right) \right\}^{-1}, \frac{\rho}{c} < 1$$

The expression for L_q can be determined as follows :

$$L_q = \sum_{n=c}^{\infty} (n - c) \rho_n$$

$$= \sum_{k=0}^{\infty} k \rho_{k+c}$$

$$= \sum_{k=0}^{\infty} k \frac{\rho^{k+c}}{c^k c!} \rho_0$$

$$= \frac{\rho^{c+1}}{c! c} \rho_0 \sum_{k=0}^{\infty} k \left(\frac{\rho}{c} \right)^{k-1}$$

$$= \frac{\rho^{c+1}}{c! c} \rho_0 \frac{d}{d \left(\frac{\rho}{c} \right)} \sum_{k=0}^{\infty} \left(\frac{\rho}{c} \right)^k$$

$$= \frac{\rho^{c+1}}{(c-1)!(c-\rho)^2} \rho_0$$

Because $\lambda_{\text{eff}} = \lambda$, $L_s = L_q + \rho$. Thus values of W_s and W_q can be determined by dividing L_s and L_q by λ (Hamdy Taha, operation reseach p.579, 2007)

In our model the interarrival truck is $\lambda = 1$ truck / hour and service time is Triangular distribution (30,60,90) / 3 so our average service rate (μ) 1 truck / hour, and we have three c (server) (inbound door facility) and result is :

Notation

λ = Average arrival rate

μ = Average speed of service

P_0 = probability of a service facility is busy or the facility utilization factor

L_s = The average amount in the system (in the queue and being served)

L_q = The Average queue length

W_s = Average time in system

W_q = Average waiting time in queue

Random interarrival and service times are described quantitatively in queueing models by **exponential distribution**, which is defined as (hamdy taha operation reseach p.549, 2007)

$$P(t \leq T) = 1 - e^{-\lambda t}, t > 0$$

Where

λ = Average Arrival in time t

t = time occurrence

2.4 Simulation

Simulation refers to a broad collection of methods and applications to mimic the behavior a real system, usually on a computer with appropriate software (Kelton *et al*, 2007). Tayfur Altiok and Benjamin Melamed, 2007 say that Simulation modeling refers to Systems and Models.

System is combination of components that act together to perform a function not possible with any of the individual parts (IEEE).

Model is the enterprise of devising a simplified representation of a complex system with the goal of providing predictions of the system's performance measure of interest (Tayfur altiok, Benjamin Melamed 2007). Simply a model is designed to capture certain behavioral aspects of the modeled system (Morris 1967) in order to gain knowledge and insight into the system's behavior.

2.4.1 type of simulation (hamdy taha, operation reseach, 2007 p. 607)

1. Continous model deals with systems whose behaviour changes *continuously* with time. A typical example the study of world population dynamics
2. Discrete models delas with the study waiting lines, with the objective of determining such mesures as the average waiting time and length of the queue. These mesure

change only when an entity enters or leaves the system. The instants at which changes take place occur at specific discrete points in time (arrival and departure events), giving rise to the name **discrete event simulation**.

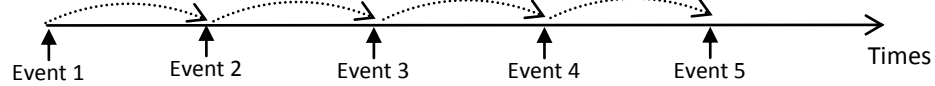


Figure 2.3 Example of occurrence of simulation events on the time scale

2.5 Arena®

Arena is discrete event simulation produced by Rockwell Software. The software uses graphical user interface that allows modelers to place modules in the workspace to represent different events or activities through which entities or objects of the model move and interact. The modules used to create the model used in this research include. The engine of Arena® is SIMAN language. Having a simulation language as its engine makes Arena models run extremely fast and makes it possible to model any complex process, such as production process, inventory management or transportation problem. Arena reputation is twenty four (24) year leading the simulation industry, taught in most universities that offer industrial Engineering or systems Engineering. Each year, more than thirty thousand (30,000) students who have studied Arena for their graduation. (www.arenasimulation.com/user).

Couple of features in the Arena® Simulation.

2.5.2 Input Analyzer

The Input Analyzer is provided as a standard component of the Arena environment. This powerful and versatile tool can be used to determine the quality of fit of probability distribution functions to input data. It may also be used to fit specific distribution functions to a data file to allow you to compare distribution functions or to display the effects of changes in parameters for the same distribution. In addition, the Input Analyzer can generate sets of random data that can then be analyzed using the software's distribution-fitting features. To run the *Input Analyzer*, double-click on the *Input Analyzer* icon or select the Input Analyzer command from the Tools menu in Arena.

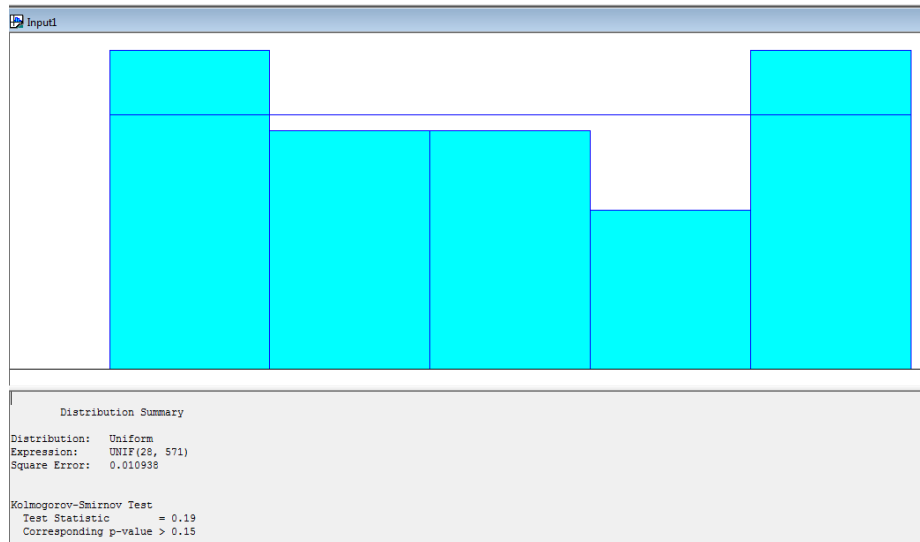


Figure 2.2 screen Input Analyzer for Uniform Distribution

2.5.2 Output Analyzer

The Output Analyzer component of Arena provides an easy-to-use interface that simplifies data analysis and allows you to view and analyze your data quickly and easily.

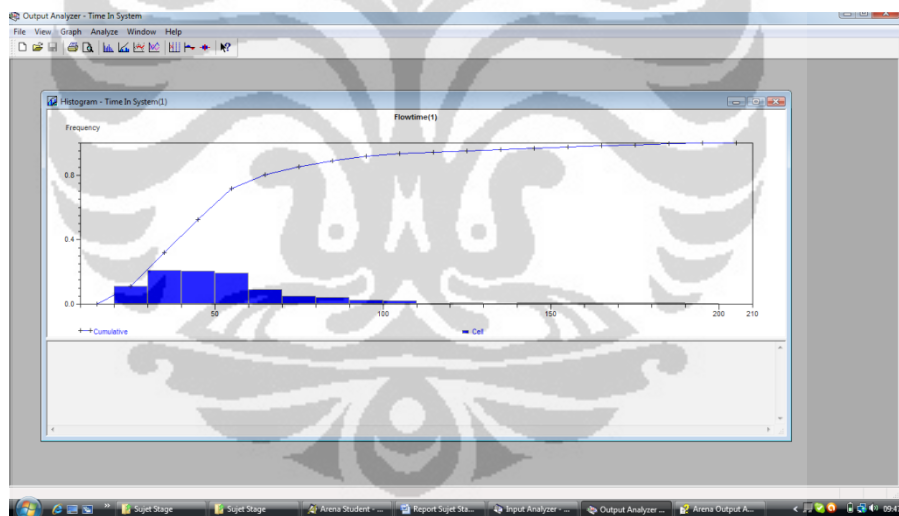


Figure 2.3 Screen Output Analyzer Histogram

2.3.3 OptQuest for Arena

OptQuest's explorer interface displays the hierarchical structure of the components of an optimization problem. OptQuest enhances Arena by automating the search for an optimal strategy (OptQuest Module 2011).

An optimization model in OptQuest for Arena has three major elements: Controls, Response, Constraints and an Objective. Controls are variables or resources in our model such as the number of machines of each type in a job shop. Responses can be used to create constraint expressions and objective expressions. Some condition before using OptQuest for Arena :

1. Model must have variable or resources . If the model has no variables or resources defined this message will appear “The Arena model has no controls defined. The model must have at least one control to run an optimization “. For example, a flowchart type model with only a Create, Delay and Dispose modules can not be optimized.
2. If the Decimal Symbol parameter defined for the machine is set to a comma instead of a period. To check this go to Start/Settings/Control Panel and click on the Regional and Language Options icon and under Regional Options click on the Customize button, there you will be able to define the Decimal Symbol to a period "." instead of a comma ",".



Chapter 3. Model approach and Assumptions

3.1 Model Approach

The crossdock operation is broken down into three major components : Inbound, Staging, Outbound. Retailer submit their order to suppliers. Following are some of the assumptions that are made related to these components.

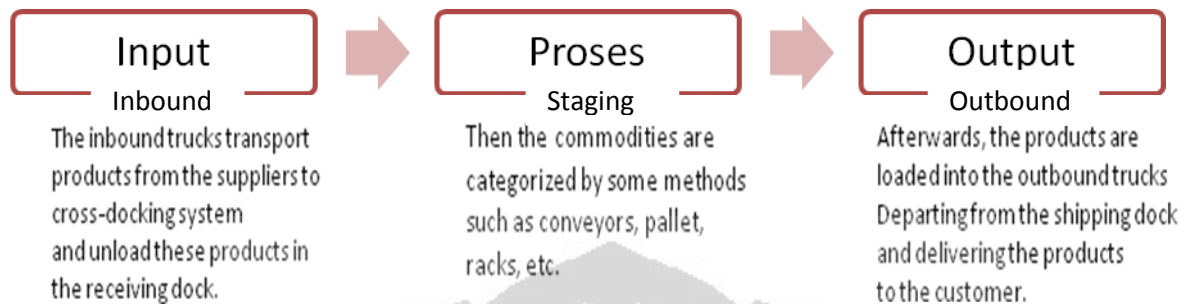


Figure 3.1 Crossdock system

Inbound

The inbound doors are assigned to fixed locations there is three Inbound door . The trucks are assumed to be docked and ready for unloading. The interarrival trucks EXPO (1) hour. The mix of freights is generated randomly UNIF (10,22) the average service time (discharge pallet) Triangular distribution with mean 1 truck per hour. Each Supplier have one single product to discharge to the crossdock and then consolidates their orders and load it to truckloads with plusieur product. There workers transfer products to outbound for delivery to individual stores, so that outgoing trucks contain plusieur products to customer. The destination and quantity of product is assigned in staging area. Which means that a given products is assigned to the fix outdoor. One forklift is allocated to one Inbound truck with activity load pallet needs time 0.5 minutes and unload pallet needs time 0.5 minutes , and distance from Inbound to Outbound Area is 75 ft.

Staging

Each destination trailer door has independent staging space of its own. Items are staged on the floor in a single layer and have resources to scanning every pallets came before delivered to outbound door. No racks are used for storage. Medium size of forklift with a weight capacity 5000 lb and velocity 75 ft / minutes with or without freight. One forklift is allocated to one pair of inbound and outbound doors. This practice avoids more than one forklift working on the same trailer

resulting in congestion in front of that door. In staging process time spent average EXPO (0.5) minutes.

Outbound

The outbound trailer door locations are fixed. An equal outbound demand scenario has been assumed (Taylor and Noble, 2004), where all outbound locations have equal freight flows. The dimensions of the trailer considered are 7.6 ft width, 7.6 ft height and 20 ft depth. Trucks will bring plusieur product that already assigned in staging area.

3.2 Assumption

This model illustrates cross dock operation, using the notion of station, entity routing among stations, entity moved from inbound to outbound trucks by Forklift, and the control of forklifts movements using distance from inbound door to outbound door and speed's forklift, at which trucks arrive and unload UNIF (10,22) pallets. Facility has three inbound door and three outbound door that have equal probability.

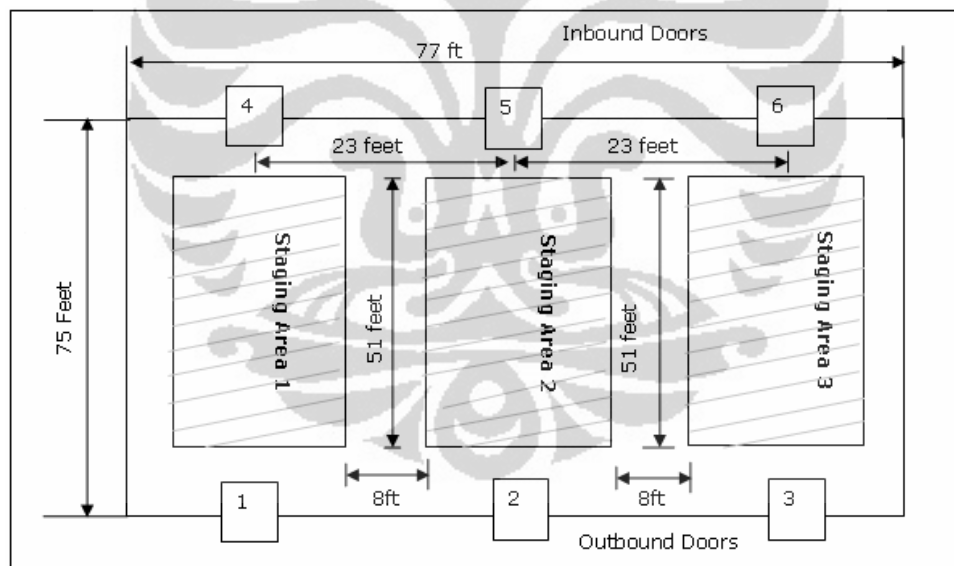


Figure 3.1 Example crossdock dimension (Sumit Nadal, 2005)

3.3 Schema Flow Process

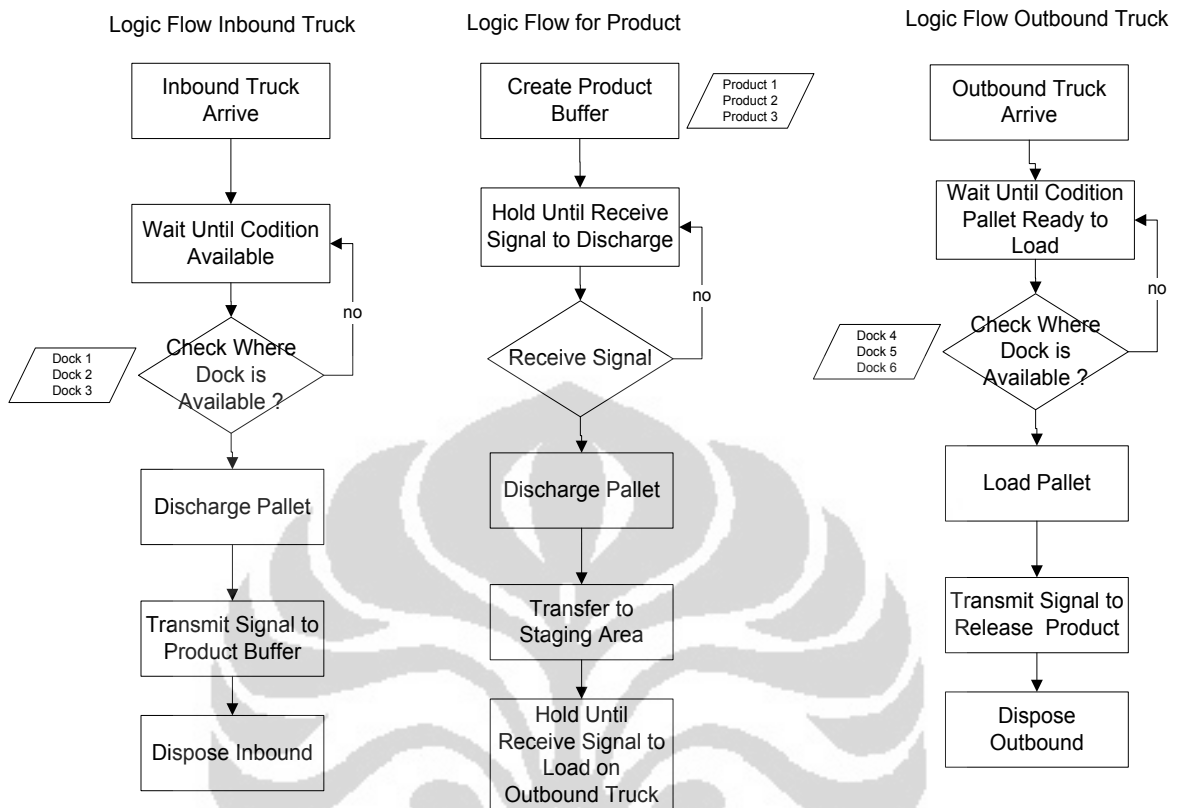
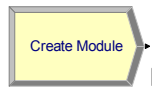


Figure 3.3. Flow process cross dock operation

3.4.4 Function of module used

The crossdock model in Arena is built with the following modules as they fall under different components of the crossdock operation :



(Basic Process)

Function : Used as a source to generate new entities, and release them into the model.

The entities (Trucks) are created in the **create module**. The time between arrival UNIF (30,60) minutes and connected with connector to signal module



(Advance Process)

Function : Used to send a signal to each hold module in the model where the value of the type parameter is *wait for signal*, in order to release the maximum specified number of entities.

The Signal modules represents the give the signal when truck arrive it will unload pallet UNIF(10,22)



(Basic Process)

Function : Used as the exit point of entities from a simulation model. Entities arrive at The **Dispose module** are disposed of and removed from the model.



(Advance Process)

Function : Used to hold an entity in a queue to either wait for a signal, wait for a specified condition to become true. The Hold module is waiting signal from signal module to unload pallets with rule Uniform distribution it is defined by two parameters Minimum and maximum (10, 22).

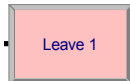
Thus far, entity transfers were implemented via Arena connections (for instantenous transfer) and *Delay* modules (for time-lapse transfer). The *Advance Transfer* template panel provides additional mechanisms of time-lapse transfer of entities among sets of modules or geographic locations. This section briefly reviews the facilities provided by this template panel.

The *Advanced Transfer* template panel implements a worldview in which entities are transported among *Station* modules. The simplest transfer mechanism uses *Route* modules as dispatch points and *Station* modules as destination points. Additionally, the *Enter* and *Leave* modules may be used to transfer entities into and out of physical or logical locations.



(Advance Transfer)

Fuction : The **Station module** The Station module defines a station (or a set of stations) corresponding to a physical or logical location where processing occurs. If the Station module defines a station set, it is effectively defining multiple processing locations.



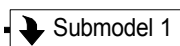
(Advance Transfer)

The **Leave module** The Leave module is used to transfer an entity to a station or module. An entity may be transferred in one of two ways: it can be transferred to a module that defines a station by referencing the station and routing, conveying, or transporting to that station or a graphical connection can be used to transfer an entity to another module.



(Advance Transfer)

The **Enter module** The Enter module defines a station (or a set of stations) corresponding to a physical or logical location where processing occurs. If the Enter module defines a station set, it is effectively defining multiple processing locations. The station (or each station within the defined set) has a matching Activity Area that is used to report all times and costs accrued by the entities in this station. This Activity Area's name is the same as the station. If a parent activity area is defined, then it also accrues any times and costs by the entities in this station. When an entity arrives at an Enter module, an "unloading" delay may occur and any transfer device used to transfer the entity to the Enter module's station may be released.



The **Sub Model** The use of submodels in your model not only increases the amount of workspace you have in which to build your model, but it also allows you the ability to better organize your model. Each submodel is represented in its own view, allowing you to partition visually a complex model flowchart into natural, easy-to-manipulate windows. Submodels themselves can contain deeper submodels; there is no limit to the amount of nesting that can occur.

3.3. Building Model Crossdock in Arena® - Modules

The basic from building this model in Arena models are modules. These are the objects that helps define process to be simulated (Kelton, et al.,2004). A schematic representation of the layout of our Cross dock facility is depicted in figure 3.2.

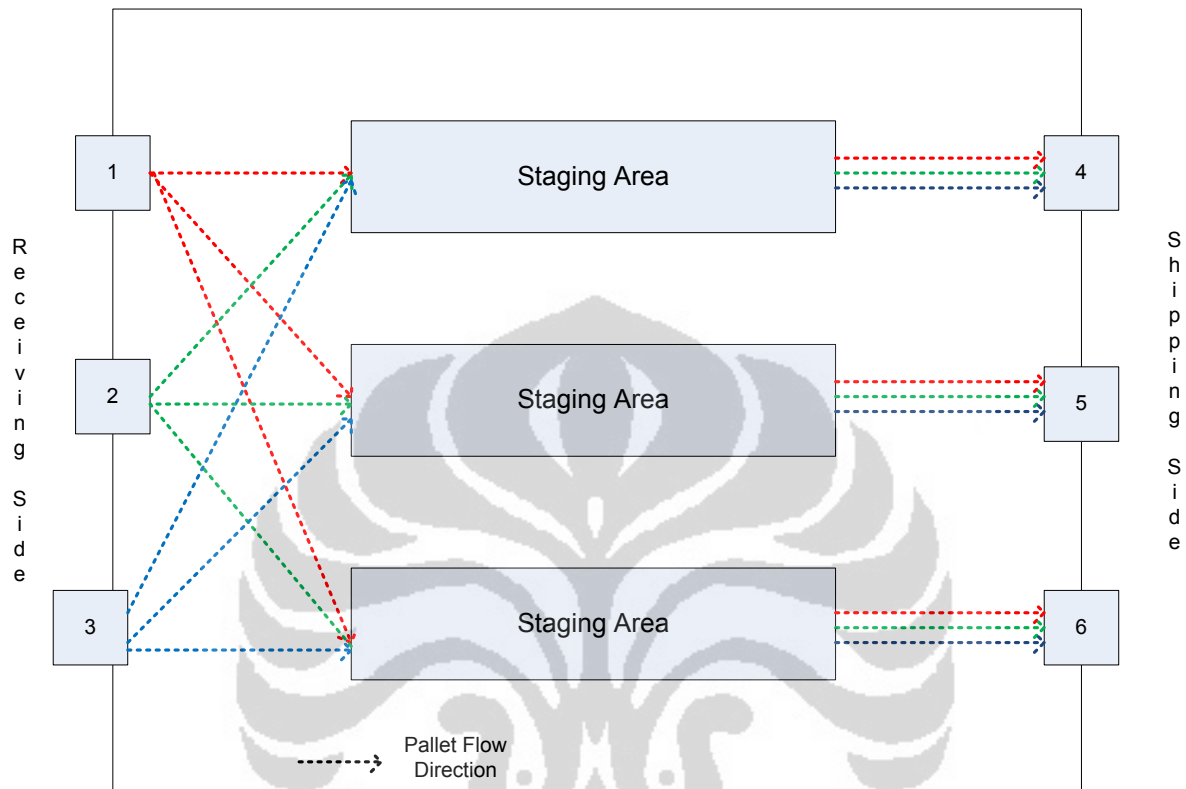


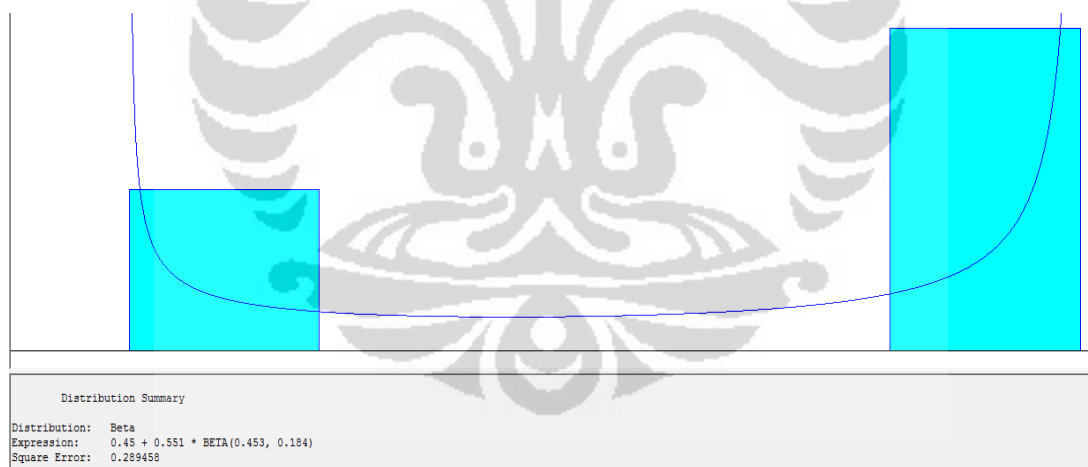
Figure 3.2 Pallet Flow Diagram

3.4 Step by Step in making Crossdock simulation with Arena® Simulation

1. Make observations at the real system, the required equipment:
 - a. Stop watch
 - b. Paper + stationery
2. Record hours of the arrival of the truck one by one into the system during the hours of operation crossdock
3. Record the time process in the Dock truck during hours of operation

Apply using the distribution fitting *Input Analyzer* for example

08h00-10h00	2	This means that in one hour there is 1 truck
10h00-12h00	2	This means that in one hour there is 1 truck
12h00-14h00	1	This means that in one hour there are 0.5 trucks
14h00-16h00	2	This means that in one hour there is 1 truck
16h00-18h00	2	This means that in one hour there is 1 truck
18h00-20h00	1	This means that in one hour there are 0.5 trucks
Total	10	λ per hour = 1,1,0.5,1,1,0.5

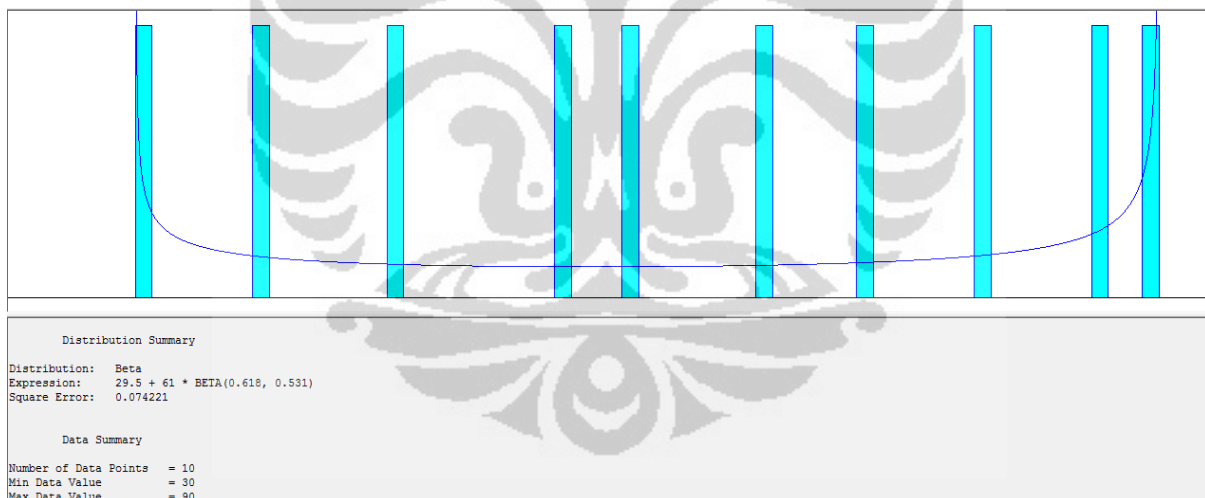


Distribution: Beta
 Expression: 0.45 + 0.551 * BETA (0.453, 0.184)
 Square Error: 0.289458 → interarrival rate λ

Now do the recording time of service, for example

Truck 1	59"	This means that in 1 hour its service rate 1.01 truck
Truck 2	73"	This means that in 1 hour its service rate 1.22 truck
Truck 3	80"	This means that in 1 hour its service rate 1.33 truck
Truck 4	37"	This means that in 1 hour its service rate 1.62 truck
Truck 5	30"	This means that in 1 hour its service rate 2 truck
Truck 6	90"	This means that in 1 hour its service rate 0.66 truck
Truck 7	45"	This means that in 1 hour its service rate 1.33 truck
Truck 8	55"	This means that in 1 hour its service rate 1.09 truck
Truck 9	87"	This means that in 1 hour its service rate 0.69 truck
Truck 10	67"	This means that in 1 hour its service rate 0.89 truck
Total	623"	μ per hour = 1.01, 1.22, 1.33, 1.62, 2, 0.66, 1.33, 1.09, 0.69, 0.89

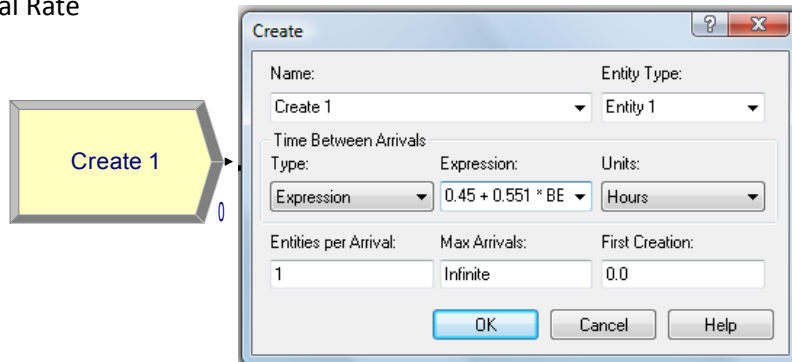
59, 73, 80, 37, 30, 90, 45, 55, 87, 67



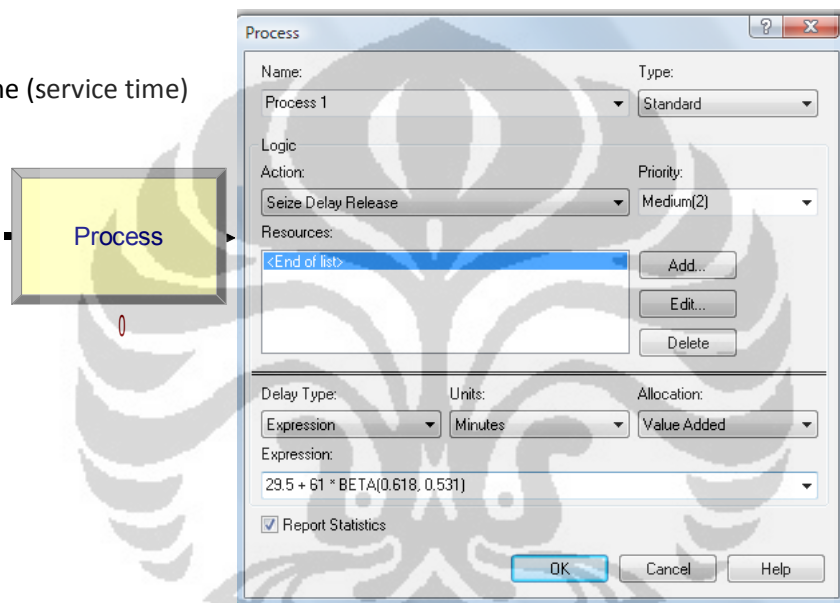
Distribution: Beta
 Expression: 29.5 + 61 * BETA (0618, 0531) minutes
 Square Error: 0.074221 → μ or delay time (processing time)

Furthermore, entering the data into the Arena simulation

Our Interrarrival Rate



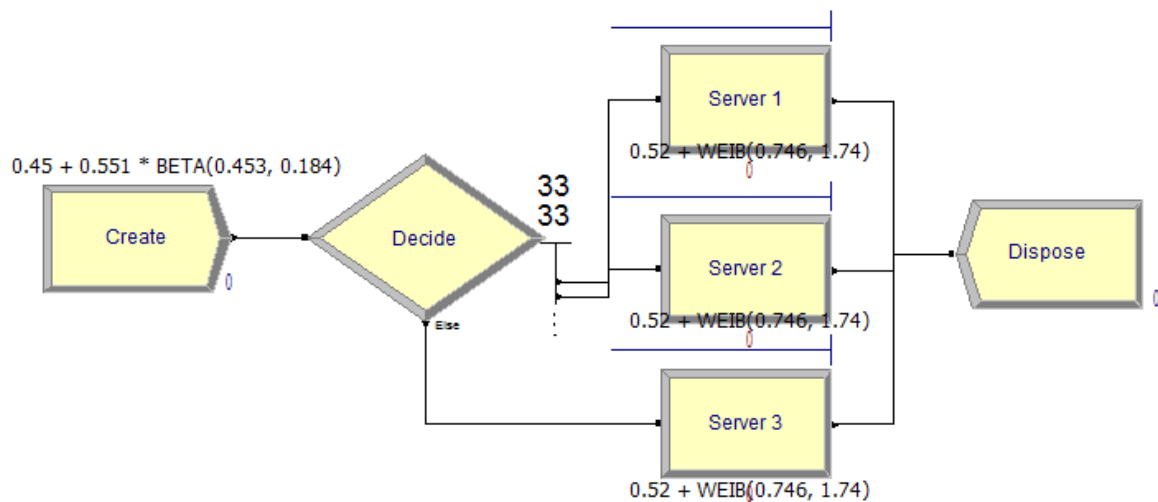
Our Delay Time (service time)



After that we can find the probability of utilization, queue number, time in queue and the total time the entity with the help of software ready to use TORA. With her input the data interarrival rate per hour $(1 + 1 + 0.5 + 1 + 1 + 0.5 / 6) = 0,833 / \text{hour}$ and the service rate $(1.01 + 1.22 + 1.33 + 1.62 + 2 + 0.66 + 1.33 + 1.09 + 0.69 + 0.89 / 10) = 1.18 / \text{hour}$

Comparative analysis									
Scenario	c	Lambda	Mu	L'da eff	p0	Ls	Lq	Ws	Wq
1	3	0.83000	1.18000	0.83000	0.49345	0.71484	0.01145	0.86125	0.01380

These results are as a comparison before running the simulation. and this way allows us to validate the model because we had already knew the results (estimates) of our system before the system is actually run.



Run

Our simulation result

Identifier	Average	Half-width	Minimum	Maximum	# Replications
Entity 1.NumberIn	14.933	.32421	14.000	17.000	30
Entity 1.NumberOut	13.200	.26673	12.000	15.000	30
Resource 1.NumberSeized	4.9333	.64990	1.0000	8.0000	30
Resource 1.ScheduledUtilization	.42271	.07361	.09526	.93444	30
Resource 2.NumberSeized	4.2666	.59588	1.0000	7.0000	30
Resource 2.ScheduledUtilization	.40343	.05903	.12127	.72507	30
Resource 3.NumberSeized	5.4333	.73820	2.0000	9.0000	30
Resource 3.ScheduledUtilization	.52152	.07232	.12535	.85889	30
System.NumberOut	13.200	.26673	12.000	15.000	30

Simulation run time: 0.02 minutes.
Simulation run complete.

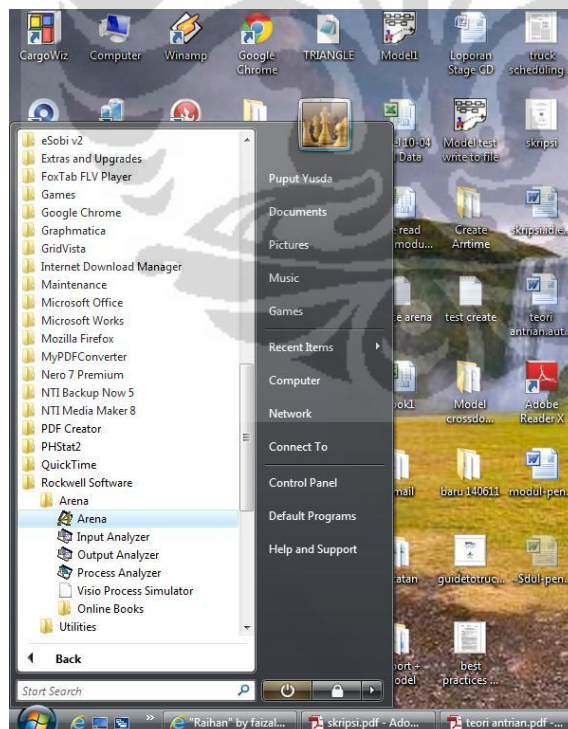
DISCRETE-CHANGE VARIABLES					
Identifier	Average	Half width	Minimum	Maximum	Final value
Entity 1.WIP	1.7843	(Insuf)	.00000	3.0000	2.0000
Resource 1.NumberBusy	.60846	(Insuf)	.00000	1.0000	1.0000
Resource 1.NumberScheduled	1.0000	(Insuf)	1.0000	1.0000	1.0000
Resource 1.Utilization	.60846	(Insuf)	.00000	1.0000	1.0000
Resource 2.NumberBusy	.60690	(Insuf)	.00000	1.0000	.00000
Resource 2.NumberScheduled	1.0000	(Insuf)	1.0000	1.0000	1.0000
Resource 2.Utilization	.60690	(Insuf)	.00000	1.0000	.00000
Resource 3.NumberBusy	.12789	(Insuf)	.00000	1.0000	.00000
Resource 3.NumberScheduled	1.0000	(Insuf)	1.0000	1.0000	1.0000
Resource 3.Utilization	.12789	(Insuf)	.00000	1.0000	.00000
Server 1.Queue.NumberInQueue	.14891	(Insuf)	.00000	1.0000	1.0000
Server 2.Queue.NumberInQueue	.29218	(Insuf)	.00000	1.0000	.00000
Server 3.Queue.NumberInQueue	.00000	(Insuf)	.00000	.00000	.00000

TALLY VARIABLES						
Identifier	Average	Half width	Minimum	Maximum	Observations	
Entity 1.VATime	70.140	(Insuf)	41.556	131.12	13	
Entity 1.NVATime	.00000	(Insuf)	.00000	.00000	13	
Entity 1.WaitTime	21.481	(Insuf)	.00000	71.717	13	
Entity 1.TranTime	.00000	(Insuf)	.00000	.00000	13	
Entity 1.OtherTime	.00000	(Insuf)	.00000	.00000	13	
Entity 1.TotalTime	91.621	(Insuf)	41.556	182.63	13	
Server 1.Queue.WaitingTime	14.024	(Insuf)	.00000	51.505	6	
Server 2.Queue.WaitingTime	35.061	(Insuf)	.00000	71.717	6	
Server 3.Queue.WaitingTime	.00000	(Insuf)	.00000	.00000	2	

TALLY VARIABLES						
Identifier	Average	Half width	Minimum	Maximum	Observations	
Entity 1.VATime	70.140	(Insuf)	41.556	131.12	13	
Entity 1.NVATime	.00000	(Insuf)	.00000	.00000	13	
Entity 1.WaitTime	21.481	(Insuf)	.00000	71.717	13	
Entity 1.TranTime	.00000	(Insuf)	.00000	.00000	13	
Entity 1.OtherTime	.00000	(Insuf)	.00000	.00000	13	
Entity 1.TotalTime	91.621	(Insuf)	41.556	182.63	13	
Server 1.Queue.WaitingTime	14.024	(Insuf)	.00000	51.505	6	
Server 2.Queue.WaitingTime	35.061	(Insuf)	.00000	71.717	6	
Server 3.Queue.WaitingTime	.00000	(Insuf)	.00000	.00000	2	

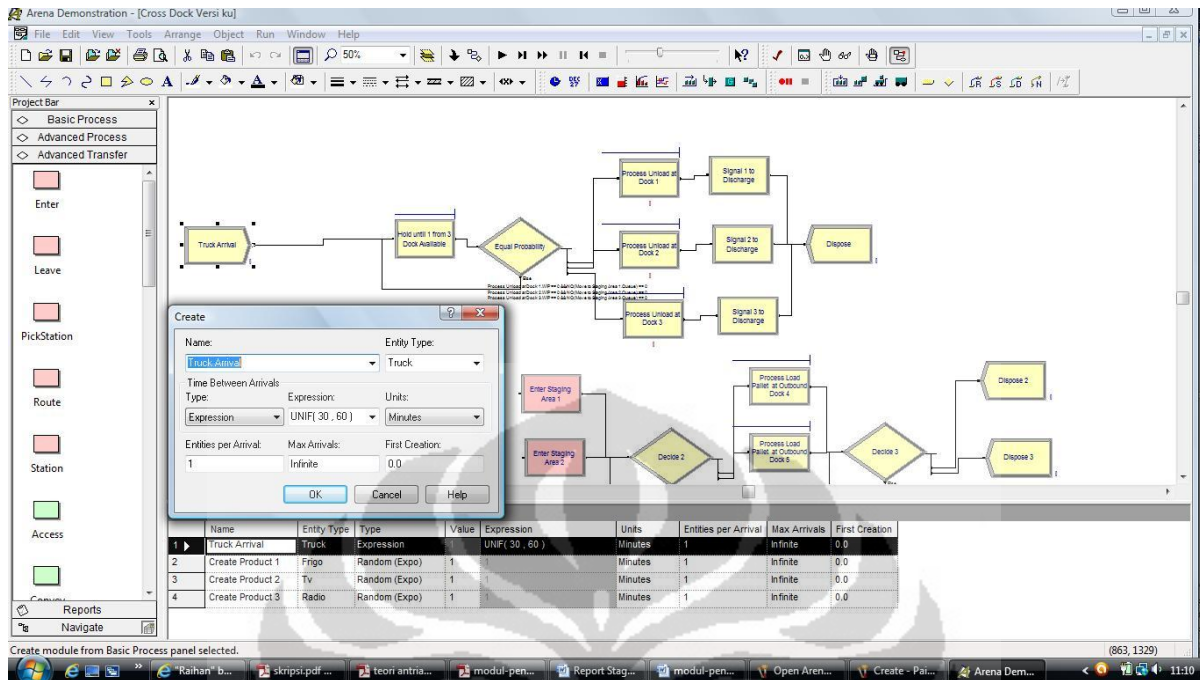
Since we already have a guidance we can modified our model

1. Open Arena Program

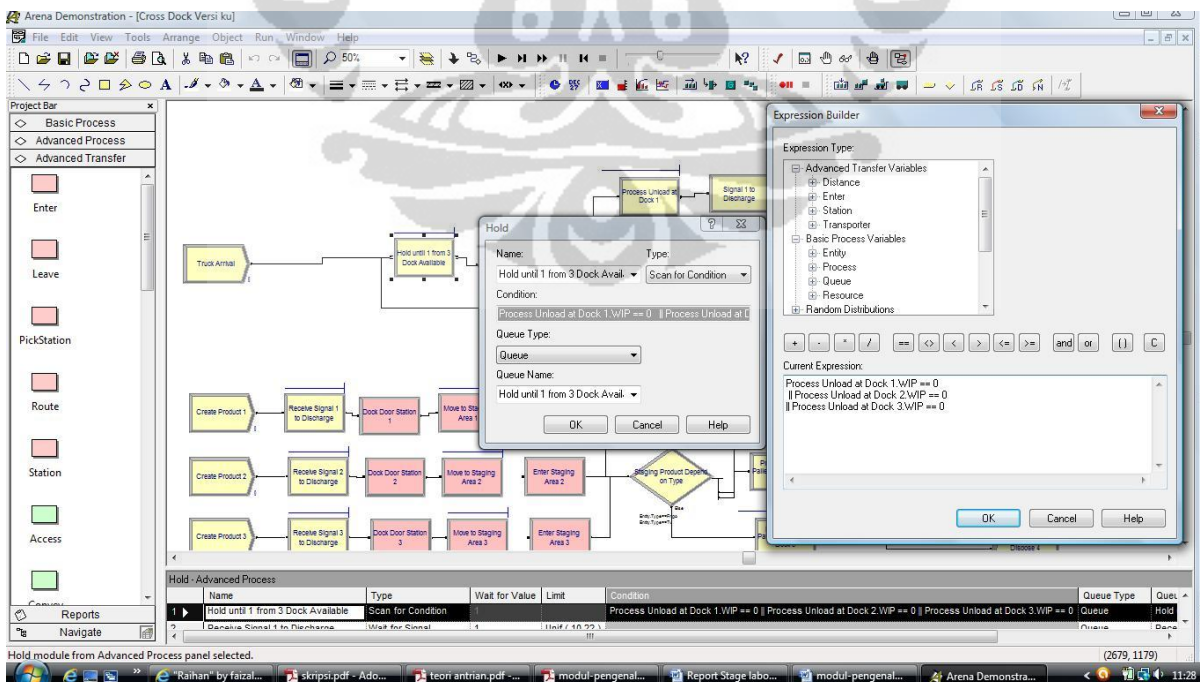


3.4.1 Create model Logic for truck Arrival

1. Firstly we *create* truck arrival and defined the time between arrival, for knowing the distribution we can use Input Analyzer, we will discuss about it after this chapter.

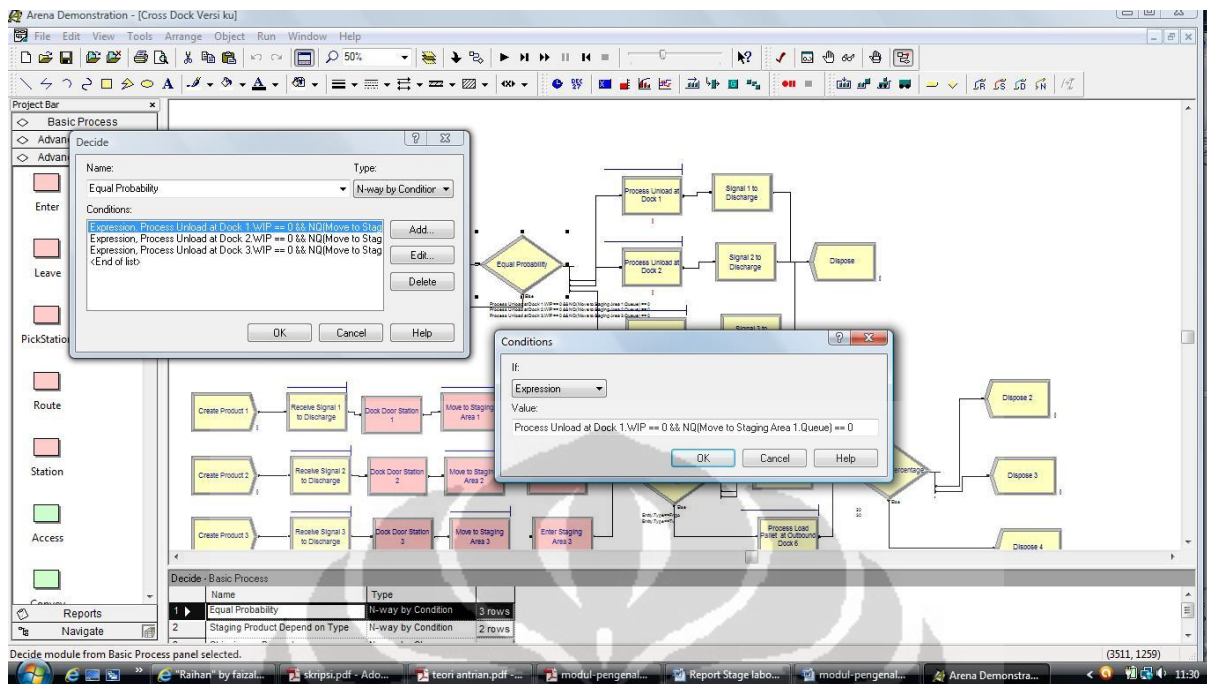


1. *Hold Module* with scan for condition this module has function to scan the dock door and transporter available condition true if `Process Unload at Dock 1.WIP == 0 || Process Unload at Dock 2.WIP == 0 || Process Unload at Dock 3.WIP == 0`

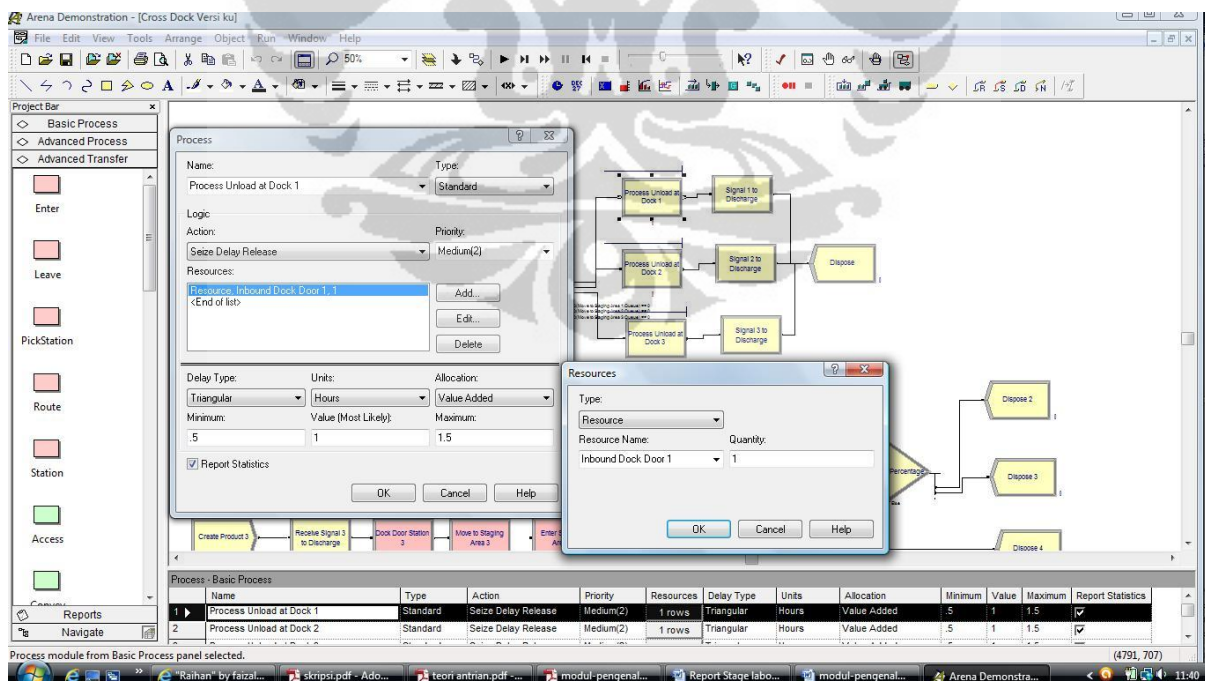


2. After that entity (truck) entering *decide module* in this module we chose *N-way by condition* and the condition is `Process Unload at Dock 1.WIP == 0 && NQ(Move to Staging`

Area 1.Queue) == 0 if the condition oke entity will enter the module true if not it will search the secondly, thirdly



- Truck processing discharge pallet in *Process Module* in *Delay Type* we assign Triangular this data we analyze from *input analyzer*



- After proces discharging pallet truck entering *Signal Module* to Transmit signal to *Hold module* which holding product until receive signal from trucks. After give signal truck enter *Dispose Module*

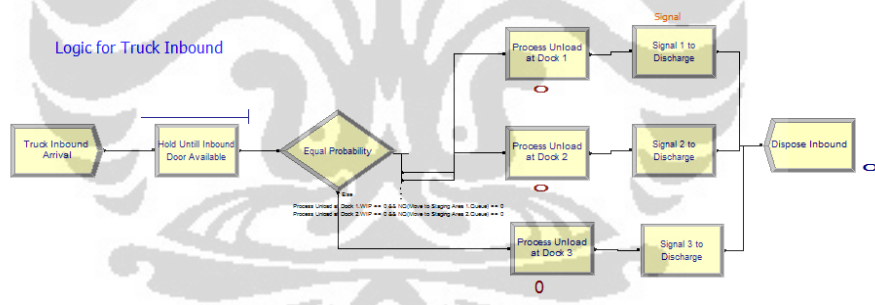
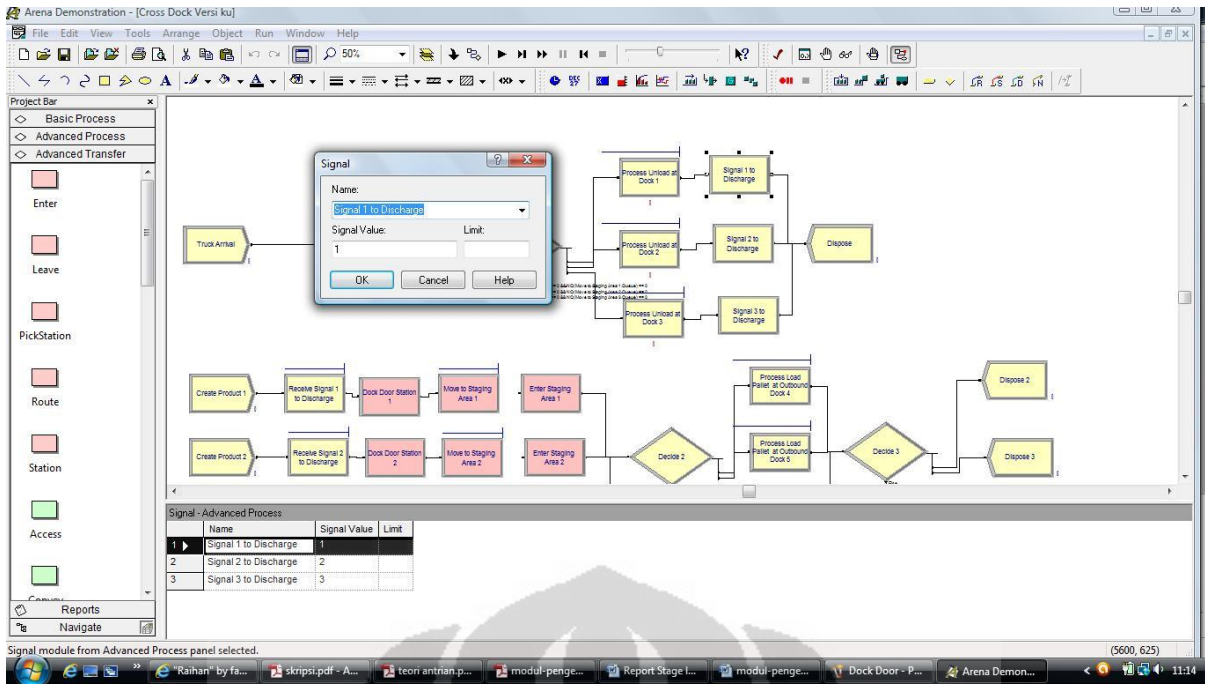
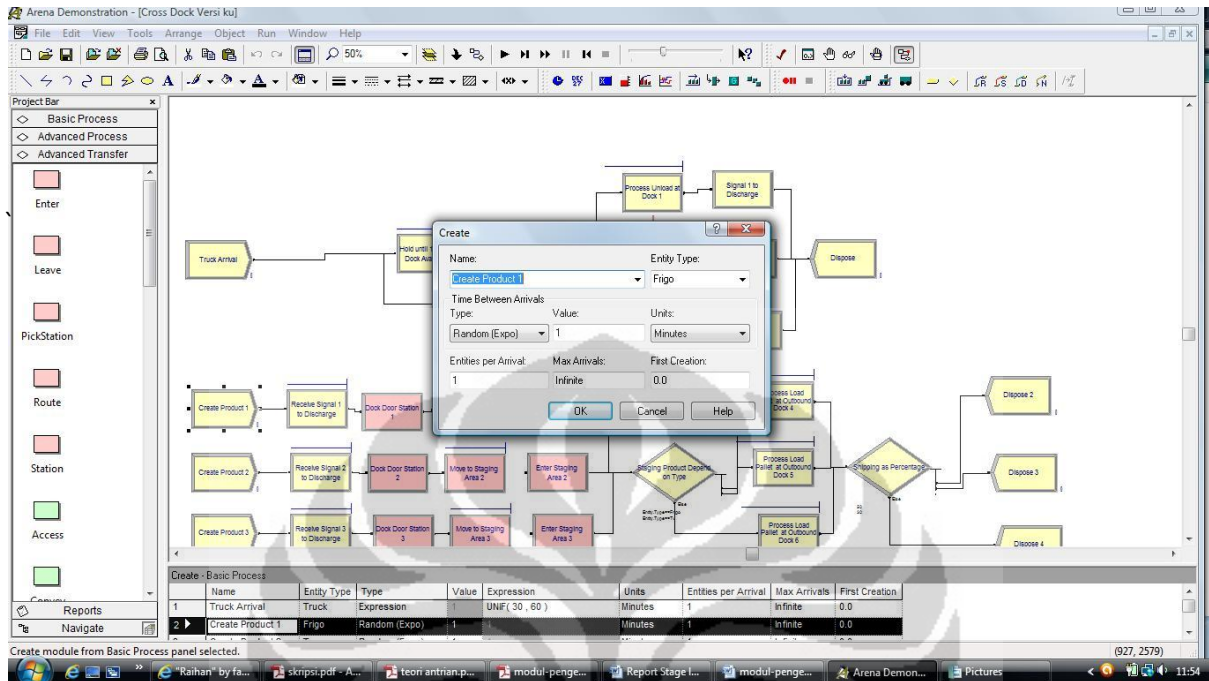


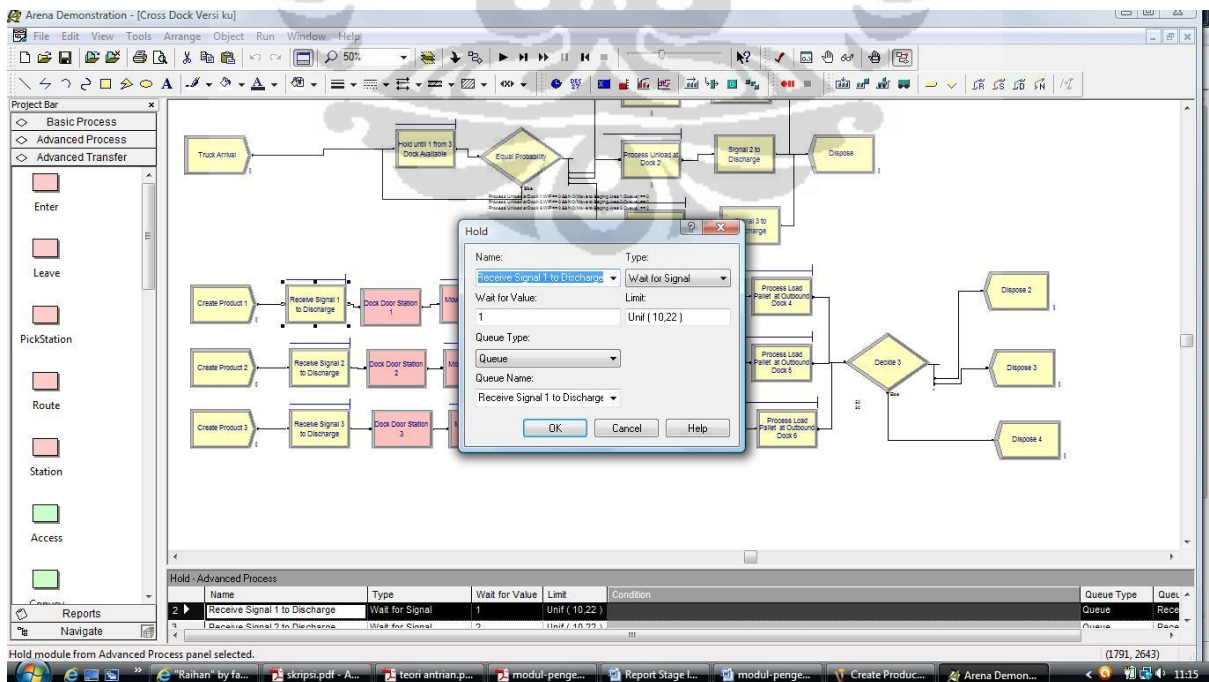
Figure 3.4.1 complete model Inbound Truck

3.4.2 Create Product to Discharge

1. Same way with create truck but in this process product created is assumed infinite but they Hold by *Hold Module* and will release if receive signal to release (we assigne limit UNIF 10,22 pallet)



2. Product wait for signal to release



3. In this module we simulate all product is already in front of dock door and ready to transfer to staging area. Forklift need 0.5 minutes to load and 0.5 minutes Unload pallet onto forklift

The screenshot shows the 'Leave' dialog box in Arena software. The dialog is configured for a 'Move to Staging Area' activity. The configuration includes:

- Name: Move to Staging Area 1
- Allocation: Value Added
- Delay: 0.5
- Units: Minutes
- Logic: (empty)
- Transfer Out: Request Transporter
- Priority: High (1)
- Queue Type: Queue
- Queue Name: Move to Staging Area 1.Queue
- Transporter Name: Forklift A
- Selection Rule: Cyclical
- Save Attribute: (empty)
- Connect Type: Transport
- Station Type: Station
- Station Name: Enter Staging Area 1.Station

The data table at the bottom of the dialog shows the configuration for three different product types:

Name	Allocation	Delay	Units	Transfer Out	Priority	Queue Type	Queue Name	Transporter Name	Selection
1 Move to Staging Area 1	Value Added	0.5	Minutes	Request Transporter	High (1)	Queue	Move to Staging Area 1.Queue	Forklift A	Cyclical
2 Move to Staging Area 2	Value Added	0	Hour	Demanded Transporter	Block (1)	Queue	Move to Staging Area 2.Queue	Forklift B	Pushed
3 Move to Staging Area 3	Value Added	0	Hour	Demanded Transporter	Block (1)	Queue	Move to Staging Area 3.Queue	Forklift B	Pushed

4. Product enter *Enter Module* it represent Station staging area where the product will stage depend on their type.

The screenshot shows the 'Enter' dialog box in Arena software. The dialog is configured for an 'Enter Staging Area' activity. The configuration includes:

- Name: Enter Staging Area 1
- Station Type: Station
- Station Name: Enter Staging Area 1.Station
- Logic: (empty)
- Delay: 0.5
- Units: Minutes
- Allocation: Value Added
- Transfer In: Free Transporter
- Transporter Name: Forklift A
- Unit Number: (empty)

The data table at the bottom of the dialog shows the configuration for three different product types:

Name	Station Type	Station Name	Parent Activity Area	Associated Intersection	Report Statistics	Delay	Allocation	Units	Transfer In
1 Enter Staging Area 1	Station	Enter Staging Area 1.Station			✓	0.5	Value Added	Minutes	Free Transporter
2 Enter Staging Area 2	Station	Enter Staging Area 2.Station			✓	0.5	Value Added	Minutes	Free Transporter
3 Enter Staging Area 3	Station	Enter Staging Area 3.Station			✓	0.5	Value Added	Minutes	Free Transporter

5. In this module the product will stage depends on their type

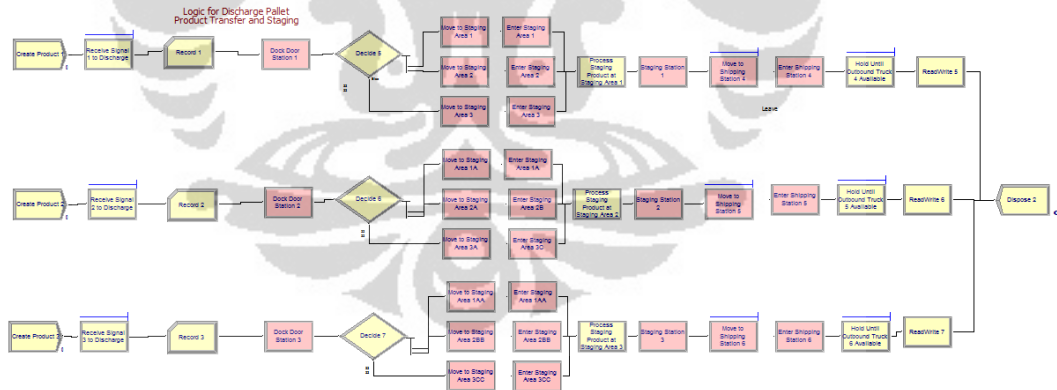
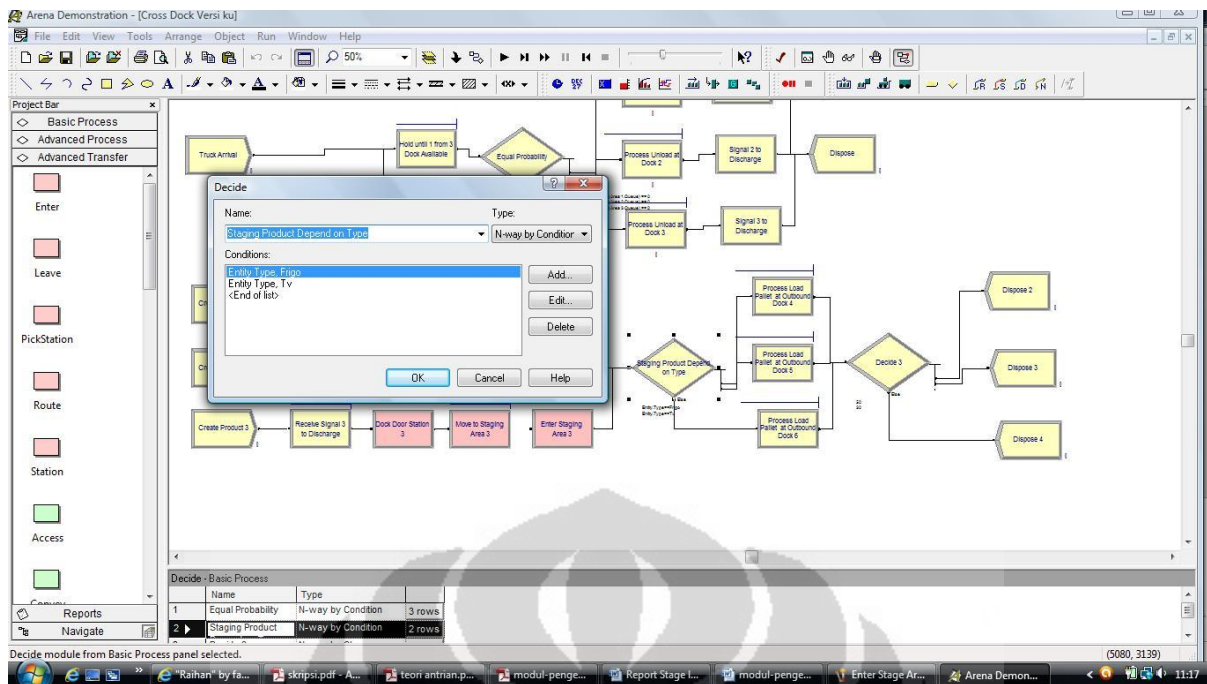
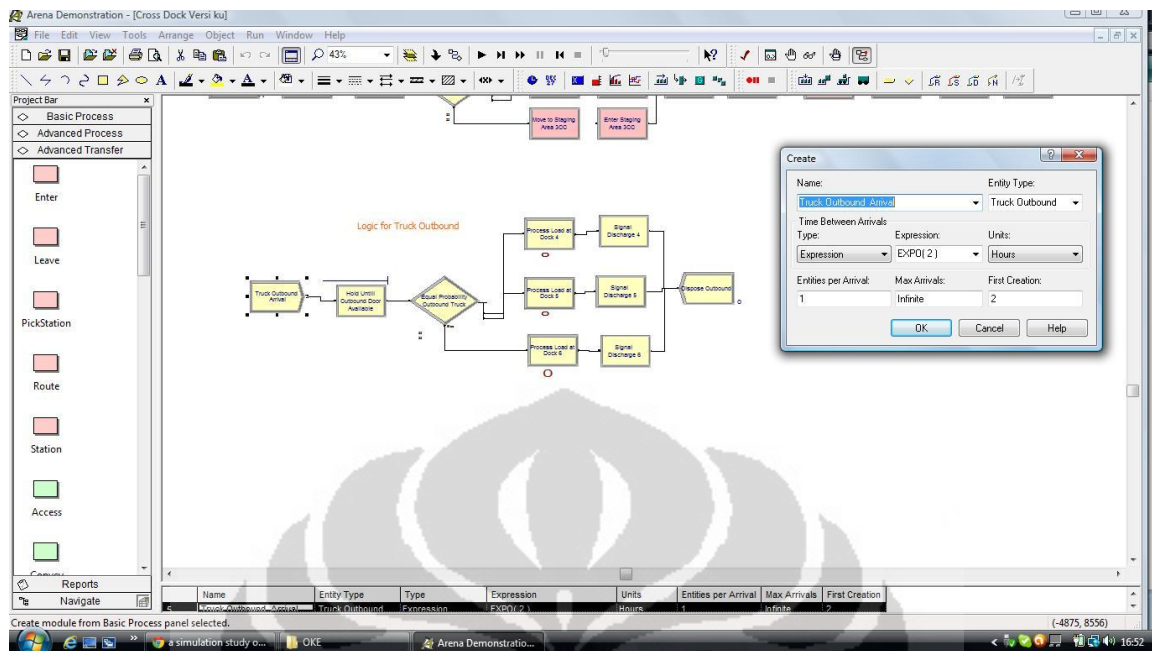


Figure 3.4.2 complete model Product Discharge and Transfer

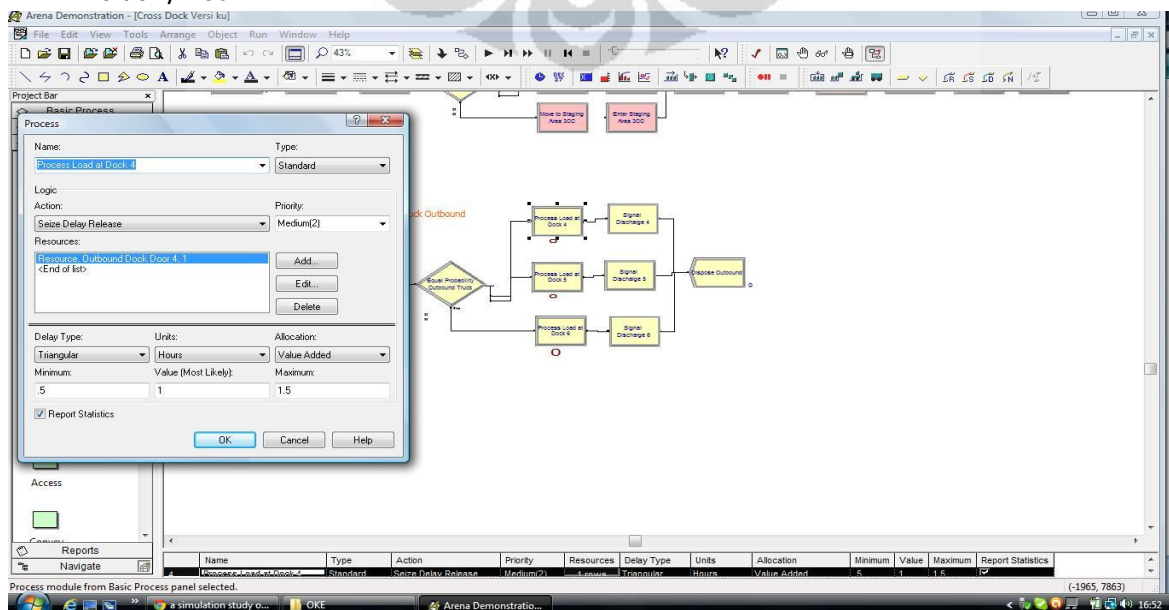
3.4.3 Trucks Outbound Arrival

1. From the *create* module we make our truck outbound. It will arrive EXPO (2) hour or else $\lambda = 0.5$ truck outbound / hour. Our first creation is after 2 hour in order to gives time for forklift finish their transfer. From the *hold* module will scan the condition is there any process in Outbound door 4, 5 or 6 if there is one available then the truck outbound will

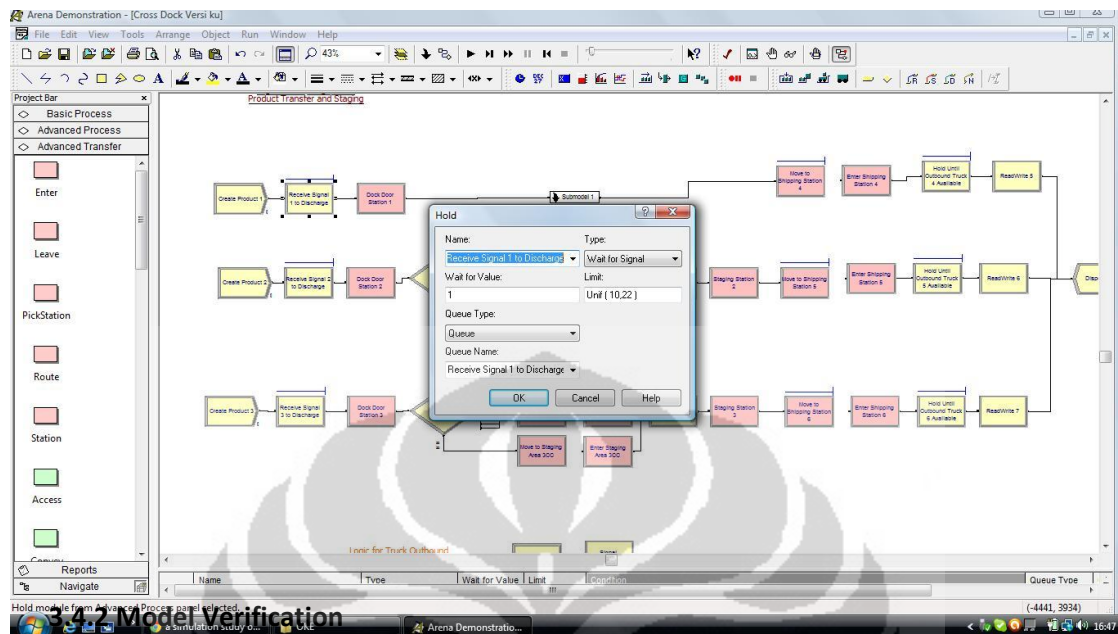
enter, but if there is no outbound door available truck will wait in hold module until it “pulls” the truck from the queue line.



- The next process is truck will entering decide module in this module truck will directed to outbound door available, we make the condition true if Process Load at Dock 4.WIP == 0 ; true if Process Load at Dock 5.WIP == 0 ; the rest go to outbound 6. Since 0 = idle and 1 = busy. Next step truck will enter the outbound door to load pallets.
- This step the truck processing to load pallets for the processing time we use Triangular Distribution with $min, mode, max$ (0.5,1,1.5) hour per truck outbound, than we have average 1 truck / hour.



- After process load pallet truck will pass signal module to order the product in *hold* module from the Shipping station we assign UNIF (10,22) pallet will load, but in this condition if there is only five pallet in the *Hold* shipping station then outbound truck only carry maximum pallet they have. Then outbound truck dispose.



Model verification is the proses ensuring that Arena model behaves in the way it was intended according to the modeling asumption made. (David Kelton *et.al* simulation with arena 3rd edition p. 300). Another way to look at verification process is to consider it as “ building the model correctly “ (Simulation Handling Book Ch.7)at least two way to make verification from Arena simulation

- Using **F4** from our keyboard
- Using *trace* from Command menu

3.4.3 Model Validation

Model validation was defined as the process ensuring that a model represents reality at a given confidence level “ building the correct model “ (Simulation Handling Book Ch.8). There are two major types of validation of interest to the simulation practitioner. The first of these is face validity. Face validity means that the model, at least on the surface, represents reality we can run our model very slowly to discover error. The second is statistical validity. Statistical validity involves a quantitative comparison between the output performance of the actual system and the model (Law and Kelton, 2000). The simulation practitioner must achieve both types of validity to have confidence that the model is accurate.

3.4.4 Model replication

The number of replication is correlated with confidence interval. Confidence interval is represent percentage of error from our point estimate in our case is (total number out truck). The simulation run is 720 Minutes with 30 replication “ why 30 “ how we can we decide $n= 30$. This is formula to search replication correlated with confidence interval for terminating system

$$X \pm t_{n-1, 1-\alpha/2} \frac{s}{\sqrt{n}}$$

n = number replication

$t_{n-1, 1-\alpha/2}^2$ = t table

for example our average sample mean (total Number out truck) from 5 replication ($n = 5$) is 13 truck with standar deviation (s) 11.3 we got *halfwidth* 7 truck, than $7/13 = 53,8\%$ error in point estimate 13 truck. If we want to achieve some spesific half-width (h) we can use the formule

$$n \cong n_0 \frac{h_0^2}{h^2}$$

Where n is the number of initial replication we have and h_0 is the half width we got. In the total number out example above, to reduce the half width from $h_0 = 7$ truck to say , $h = 3$, we'd thus need a total replication

$$n \cong 5 \frac{7^2}{3^2} = 27.2 \text{ (approximation)}$$

Chapter 4. Scenario Problem

Model of a cross-dock system that groups and transfers material for further shipment. This facility has three incoming docks and three outgoing docks. Trucks arrive at each of the incoming docks with loads of material on pallets. The interarrival time is (EXPO) 1 hour between truck arrival on each incoming dock (all times are in minutes). Each trucks will have a number of pallets drawn from a UNIF (10,22) that need to be transferred to one of outgoing docks. The processing time for discharge pallet using Triangular distribution with $min, mode, max$ (0.5,1,1.5) hour per truck. Each dock have equal probability of any incoming pallet going to any of the three outgoing docks. When trucks arrive, an resources with trolly unloading the pallets at the incoming docks. This activity require time (0.5) load and (0.5) unload for each pallets (all time are in minutes).So the pallets are transferred by Forklift one by one pallets to staging area to assign their quantity and destination. After that pallets are transferred to the outbound dock which are located on the other side of the building this activity require (0.3) load and (0.3) unload. Truck outbound assign interarrival time EXPO (2) hour and first create after 2 hour simulation to give time to pallet fully transfered. From the staging area every pallet assign to their destination dock and quantity, they (trucks) required UNIF (10,22) pallet but this difficult because transfer time take much time before arrive at outbound door. In our model we have six forklift with speed average 75 ft/minute. We run our Simulation 720 minutes with 30 replication.

In practice, transshipment has various layouts. In this research the layout is being restricted to three inbound and three outbound door. Eventhough restriction is not realistic (in a real transshipment platform) but can be used as a baseline for other layouts. In this model an incoming truck arrives at inbound door and unloads products for various destinations. If the outgoing truck is going to the fine destination, the products are moved directly to outbound truck (direct transit of products), in the other hand. In studied model, the following assumptions are considered:

- Each trailer leaves the inbound door when it is fully unloaded. On the other side, each trailer leaves the outbound door when it is fully loaded.
- The storage capacity is assumed unlimited.
- All incoming and outgoing semi trailers are available at time zero.
- The total numbers of arriving and departing products are depends on time process.
- Loading, unloading time have same distribution
- transfer time are constant and are not considered.

Chapter 5. Result and Analysis

From 720 minutes simulation we got the result truck inbound and in as a table below with average 12 truck in and 11 truck out with halfwidth 9% and 10 %

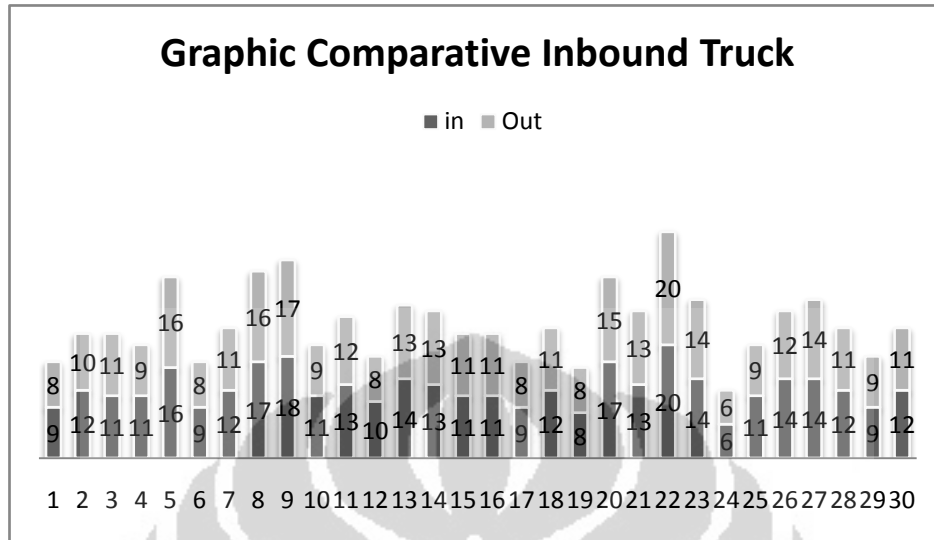


Figure 5.1 grafik comparative between Truck in and Truck out from 30 replication

From the table 5.1 we can see truck arrive at time 00 enter inbound door 1 and exit at the 55 minutes 43 second with number of pallets 20. In this activity we assumed that serve hour (row) is the time from resource complete their discharging pallets

Event	Time in (at Minute)	Dock number	Time Out	Serve Hour (discharge)	Pallet discharge
1	0	1	55''43	55''43	20
2	20''77	2	89''31	68''54	13
3	142''48	2	205''34	62''86	14
4	203''63	3	265''67	62''.04	21
5	258''17	1	314''79	56''62	11
6	268''.98	2	345''.22	76''.24	11
7	385''.06	2	454''.88	69''82	11
8	385''14	1	434''.30	49''16	18
9	403''77	3	471''21	67''44	10
10	512''.12	1	612''14	100''	18

Table 5.1 event occurrence from Inbound Dock according time simulation

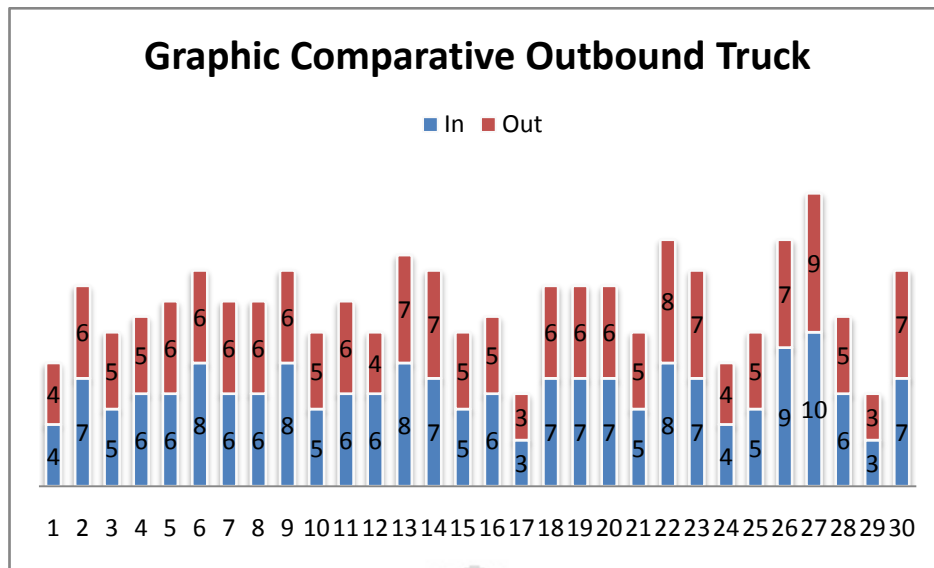


Figure 5.2 grafik comparative between Truck in and Truck out Outbound Door from 30 replication

From the Outbound dock door we have average 6 truck in and 5 truck out with halfwidth 10% and 9%

Event	Time in	Dock Number	Time Out	Serve Hour	Number Pallet Load
1	157"	6	180".9	24"	8
2	240"	4	291".7	51"	22
3	342"	5	293"	51"	14
4	501".56	5	535".5	34"	19

Table 5.2 event occurrence from Outbound Dock according time simulation

As a result utilization inbound dock from 30 replication we have inbound dock door 1 average 34.4% inbound door 2 have average 30.3 % of utilization and inbound door 3 have average 36.8% from their utilization

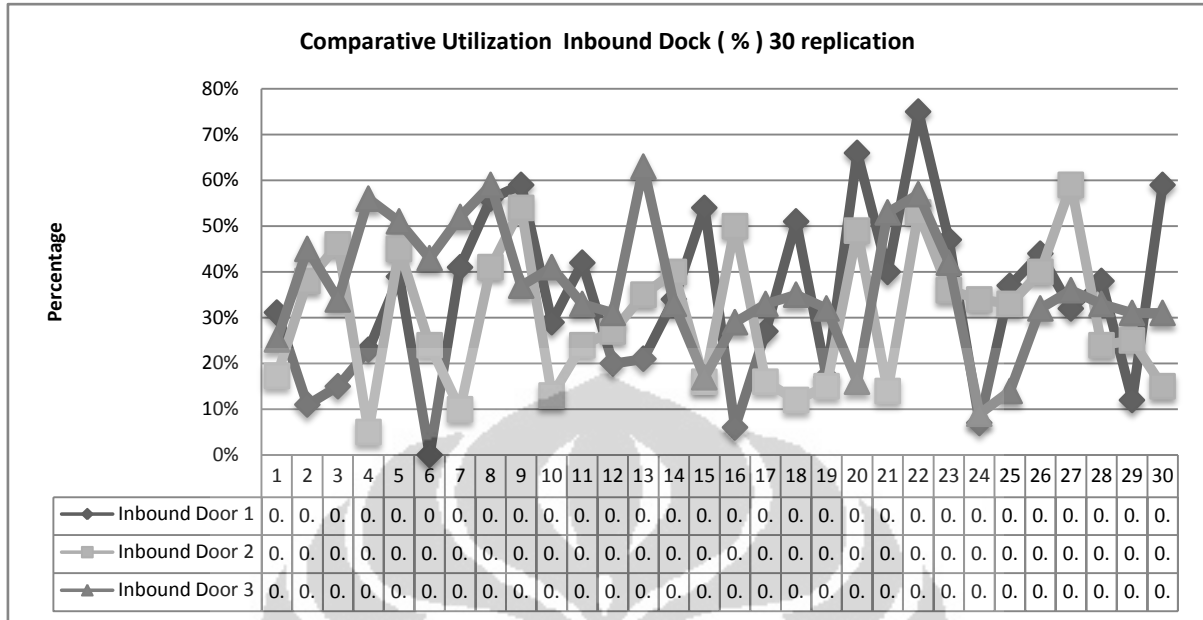


Figure 5.3 total utilization inbound door from 30 replication

Since we have six resources three forklift inbound and three forklift outbound we have average utilization 27.5 %, 17.8 % ,19.6%, for forklift inbound 1, 2, and 3. 13.9%, 13.7%, 15.7% for forklift outbound 4, 5 and 6. Almost there is no queue inside of our crossdock building.

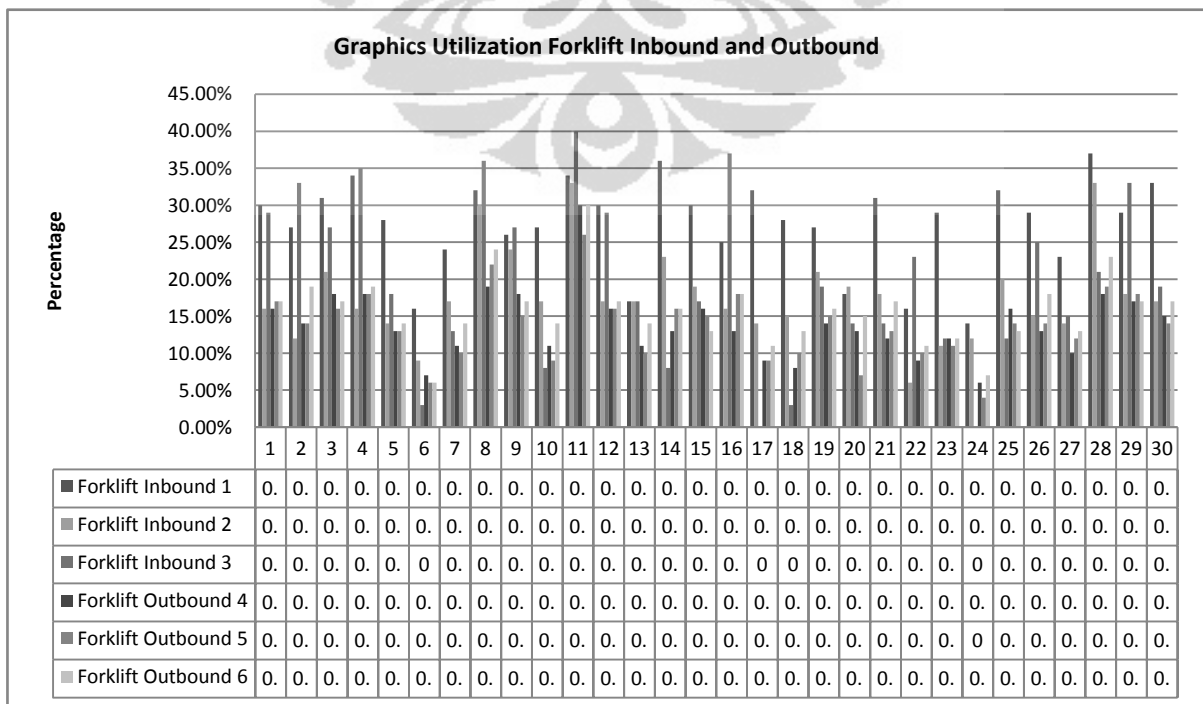
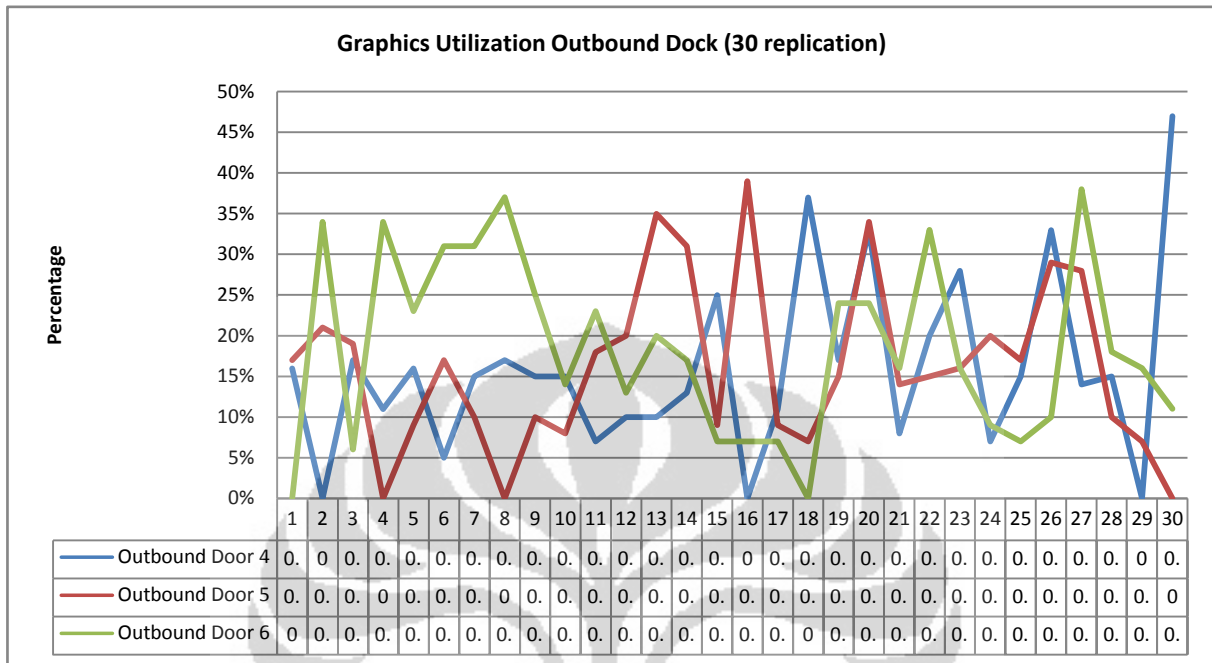


Figure 5.4 total utilization Forklift

From outbound dock we have more small utilization percentage than inbound dock. Because of in our model truck out bound first creation at time 120 minute to give time for forklift finish transfer pallet from inbound to outbound dock. Outbound bond door 4 have 15.9 % utilization, outbound dock 5 16.1 %, and 18.4 % for outbound door 6



For the total time transfer per pallet (product 1, product 2 and product 3) 1.162 minutes, 1.111 minutes, 0.958 minutes with halfwidth 0. 02498, 0.01337, and 0.1667 with percentage error is 2%, 1% and 17 %.

Chapter 6. Conclusion

We conclude that Arena simulation is one of the solving tool to analyzing problems for example problem the flow process (bottle neck), resources utilization or maybe much more advantage from Arena Simulation and that we not explore yet.

The crossdock operation is need to be planned for to optimizing our resources utilization.

Model Proposed

Since our Inbound and Outbound door is fixed, we still can arrange our resources utilization in order to more visible. Is more simple because we already know the interarrival rate and service rate from our resources, than we only have to arrange our forklift "on-call" they stand-by only call

6.1 Future reseach

There are many possibility to expand this reseach for example we can applied in bigger cross dock let say 36 inbound dock and 36 outbound dock or we can combined our queuing analysis with optmization technique, where we seek the minimization of the sum of the two cost, the cost of waiting and the cost of offering service facility.

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Appendix 1

I. Siman Language

```

;
;
;   Model statements for module:  BasicProcess.Create 1 (Truck Inbound Arrival)
;

59$   CREATE,
1,HoursToBaseTime(0.0),Truck:HoursToBaseTime(EXPO(1.5)):NEXT(60$);

60$   ASSIGN:      Truck Inbound Arrival.NumberOut=Truck Inbound
Arrival.NumberOut + 1:NEXT(58$);

58$   SCAN:
      Process Unload at Dock 1.WIP == 0 || Process Unload at
Dock 2.WIP == 0 || Process Unload at Dock 3.WIP == 0
      :NEXT(4$);

;
;
;   Model statements for module:  BasicProcess.Decide 1 (Equal Probability)
;
4$   BRANCH,      1:
      If,Process Unload at Dock 1.WIP == 0 && NQ(Move to
Staging Area 1.Queue) == 0,0$,Yes:
      If,Process Unload at Dock 2.WIP == 0 && NQ(Move to
Staging Area 2.Queue) == 0,1$,Yes:
      Else,2$,Yes;

;
;
;   Model statements for module:  BasicProcess.Process 3 (Process Unload at Dock
3)
;
2$   ASSIGN:      Process Unload at Dock 3.NumberIn=Process Unload at
Dock 3.NumberIn + 1:
      Process Unload at Dock 3.WIP=Process Unload at Dock
3.WIP+1;
68$   QUEUE,      Process Unload at Dock 3.Queue;
67$   SEIZE,      2,VA:
      Inbound Dock Door 3,1:NEXT(66$);

66$   DELAY:      HoursToBaseTime(Triangular(.5,1,1.5)),,VA;
65$   RELEASE:    Inbound Dock Door 3,1;
113$  ASSIGN:      Process Unload at Dock 3.NumberOut=Process Unload at
Dock 3.NumberOut + 1:
      Process Unload at Dock 3.WIP=Process Unload at Dock
3.WIP-1:NEXT(7$);

;
;
;   Model statements for module:  AdvancedProcess.Signal 3 (Signal 3 to
Discharge)
;
7$   SIGNAL:      3:NEXT(3$);

;
;
;   Model statements for module:  BasicProcess.Dispose 1 (Dispose Inbound)
;
3$   ASSIGN:      Dispose Inbound.NumberOut=Dispose Inbound.NumberOut +
1;
116$  DISPOSE:    Yes;

;

```

```

;
;   Model statements for module:  BasicProcess.Process 1 (Process Unload at Dock
1)
;
0$           ASSIGN:           Process Unload at Dock 1.NumberIn=Process Unload at
Dock 1.NumberIn + 1:
                                Process Unload at Dock 1.WIP=Process Unload at Dock
1.WIP+1;
120$        QUEUE,           Process Unload at Dock 1.Queue;
119$        SEIZE,          2,VA:
                                Inbound Dock Door 1,1:NEXT(118$);

118$        DELAY:           HoursToBaseTime(Triangular(.5,1,1.5)),,VA;
117$        RELEASE:        Inbound Dock Door 1,1;
165$        ASSIGN:           Process Unload at Dock 1.NumberOut=Process Unload at
Dock 1.NumberOut + 1:
                                Process Unload at Dock 1.WIP=Process Unload at Dock
1.WIP-1:NEXT(5$);

;
;
;   Model statements for module:  AdvancedProcess.Signal 1 (Signal 1 to
Discharge)
;
5$          SIGNAL:          1:NEXT(3$);

;
;
;   Model statements for module:  BasicProcess.Process 2 (Process Unload at Dock
2)
;
1$          ASSIGN:           Process Unload at Dock 2.NumberIn=Process Unload at
Dock 2.NumberIn + 1:
                                Process Unload at Dock 2.WIP=Process Unload at Dock
2.WIP+1;
171$        QUEUE,           Process Unload at Dock 2.Queue;
170$        SEIZE,          2,VA:
                                Inbound Dock Door 2,1:NEXT(169$);

169$        DELAY:           HoursToBaseTime(Triangular(.5,1,1.5)),,VA;
168$        RELEASE:        Inbound Dock Door 2,1;
216$        ASSIGN:           Process Unload at Dock 2.NumberOut=Process Unload at
Dock 2.NumberOut + 1:
                                Process Unload at Dock 2.WIP=Process Unload at Dock
2.WIP-1:NEXT(6$);

;
;
;   Model statements for module:  AdvancedProcess.Signal 2 (Signal 2 to
Discharge)
;
6$          SIGNAL:          2:NEXT(3$);

;
;
;   Model statements for module:  BasicProcess.Create 2 (Create Product 1)
;
219$        CREATE,
1,MinutesToBaseTime(0.0),Refrigerator:MinutesToBaseTime(EXPO(3)):NEXT(220$);

220$        ASSIGN:           Create Product 1.NumberOut=Create Product 1.NumberOut
+ 1:NEXT(8$);

;
;
;   Model statements for module:  AdvancedProcess.Hold 2 (Receive Signal 1 to
Discharge)

```

```

;
8$      QUEUE,      Receive Signal 1 to Discharge.Queue;
        WAIT:      1,Unif ( 10,22 ):NEXT(53$);

;
;
;      Model statements for module:  BasicProcess.Assign 4 (Assign 4)
;
53$     ASSIGN:     Arrtime P1=tnow:NEXT(10$);
;
;
;      Model statements for module:  AdvancedTransfer.Station 1 (Dock Door Station
1)
;
10$     STATION,    Dock Door 1;
225$    DELAY:      0.0,,VA:NEXT(11$);
;
;
;      Model statements for module:  AdvancedTransfer.Leave 1 (Move to Staging Area
1)
;
11$     DELAY:      0.00,,VA:NEXT(239$);
;
239$    QUEUE,      Move to Staging Area 1.Queue;
243$    REQUEST,    1:Forklift Inbound 1(CYC);
231$    DELAY:      0.5,,VA:NEXT(233$);
;
233$    TRANSPORT:  ,Enter Staging Area 1.Station;
;
;
;      Model statements for module:  AdvancedTransfer.Enter 1 (Enter Staging Area 1)
;
12$     STATION,    Enter Staging Area 1.Station;
246$    DELAY:      0.5,,VA:NEXT(248$);
;
248$    FREE:       Forklift Inbound 1:NEXT(48$);
;
;
;      Model statements for module:  AdvancedProcess.Delay 1 (Process Staging
Product at Staging Area 1)
;
48$     DELAY:      EXPO( 0.5 ),,Other:NEXT(51$);
;
;
;      Model statements for module:  BasicProcess.Assign 3 (Assign Product Type from
Inbound truck 3)
;
51$     ASSIGN:     Type=DISC ( 0.3,1,0.65,2,1,3 ):
                    Entity.Type=Types ( type ):
                    Entity.Picture=Pict ( type ):NEXT(13$);
;
;
;      Model statements for module:  BasicProcess.Decide 2 (Staging Product Depend
on Percentage)
;
13$     BRANCH,     1:
                    With, (33)/100,31$,Yes:
                    With, (33)/100,32$,Yes:
                    Else,33$,Yes;
;
;
;      Model statements for module:  AdvancedTransfer.Station 6 (Outbound Door
Station 6)
;

```

```

33$          STATION,      Outbound Door Station 6;
261$        DELAY:        0.0,,VA:NEXT(38$);
;
;
;      Model statements for module:  AdvancedTransfer.Leave 6 (Move to Shipping
Station 6)
;
38$          DELAY:        0.00,,VA:NEXT(275$);

275$        QUEUE,        Move to Shipping Station 6.Queue;
279$        REQUEST,      1:Forklift Outbound 3(CYC);
267$        DELAY:        0.5,,VA:NEXT(269$);

269$        TRANSPORT:    ,Enter Shipping Station 6.Station;
;
;
;      Model statements for module:  AdvancedTransfer.Station 4 (Outbound Door
Station 4)
;

31$          STATION,      Outbound Door Station 4;
284$        DELAY:        0.0,,VA:NEXT(34$);
;
;
;      Model statements for module:  AdvancedTransfer.Leave 4 (Move to Shipping
Station 4)
;
34$          DELAY:        0.00,,VA:NEXT(298$);

298$        QUEUE,        Move to Shipping Station 4.Queue;
302$        REQUEST,      1:Forklift Outbound 1(CYC);
290$        DELAY:        0.5,,VA:NEXT(292$);
292$        TRANSPORT:    ,Enter Shipping Station 4.Station;
;
;
;      Model statements for module:  AdvancedTransfer.Station 5 (Outbound Door
Station 5)
;
32$          STATION,      Outbound Door Station 5;
307$        DELAY:        0.0,,VA:NEXT(36$);
;
;
;      Model statements for module:  AdvancedTransfer.Leave 5 (Move to Shipping
Station 5)
;
36$          DELAY:        0.00,,VA:NEXT(321$);
321$        QUEUE,        Move to Shipping Station 5.Queue;
325$        REQUEST,      1:Forklift Outbound 2(CYC);
313$        DELAY:        0.5,,VA:NEXT(315$);
315$        TRANSPORT:    ,Enter Shipping Station 5.Station;
;
;
;      Model statements for module:  BasicProcess.Create 3 (Create Product 2)
;
328$          CREATE,
1,MinutesToBaseTime(0.0),Television:MinutesToBaseTime(EXPO(3)):NEXT(329$);

329$          ASSIGN:      Create Product 2.NumberOut=Create Product 2.NumberOut
+ 1:NEXT(14$);
;
;
;      Model statements for module:  AdvancedProcess.Hold 3 (Receive Signal 2 to
Discharge)
;
14$          QUEUE,        Receive Signal 2 to Discharge.Queue;
          WAIT:            2,Unif ( 10,22 ):NEXT(54$);
;

```

```

;
; Model statements for module: BasicProcess.Assign 5 (Assign 5)
;
54$      ASSIGN:      Arrtime P2=tnow:NEXT(16$);
;
;
; Model statements for module: AdvancedTransfer.Station 2 (Dock Door Station
2)
;
16$      STATION,      Dock Door 2;
334$     DELAY:        0.0,,VA:NEXT(17$);
;
;
; Model statements for module: AdvancedTransfer.Leave 2 (Move to Staging Area
2)
;
17$      DELAY:        0.00,,VA:NEXT(348$);

348$     QUEUE,        Move to Staging Area 2.Queue;
352$     REQUEST,      1:Forklift Inbound 2(CYC);
340$     DELAY:        0.0000000000000000,,VA:NEXT(342$);
342$     TRANSPORT:    ,Enter Staging Area 2.Station;
;
;
; Model statements for module: AdvancedTransfer.Enter 2 (Enter Staging Area 2)
;

18$      STATION,      Enter Staging Area 2.Station;
355$     DELAY:        0.5,,VA:NEXT(357$);

357$     FREE:         Forklift Inbound 2:NEXT(49$);
;
;
; Model statements for module: AdvancedProcess.Delay 2 (Process Staging
Product at Staging Area 2)
;
49$      DELAY:        EXPO( 0.5 ),,Other:NEXT(51$);
;
;
; Model statements for module: BasicProcess.Create 4 (Create Product 3)
;

366$     CREATE,      1,MinutesToBaseTime(0.0),Radio:MinutesToBaseTime(EXPO(3)):NEXT(367$);
367$     ASSIGN:      Create Product 3.NumberOut=Create Product 3.NumberOut
+ 1:NEXT(19$);
;
;
; Model statements for module: AdvancedProcess.Hold 4 (Receive Signal 3 to
Discharge)
;
19$      QUEUE,        Receive Signal 3 to Discharge.Queue;
WAIT:    3,Unif ( 10,22 ):NEXT(55$);
;
;
; Model statements for module: BasicProcess.Assign 6 (Assign 6)
;
55$      ASSIGN:      Arrtime P3=tnow:NEXT(21$);
;
;
; Model statements for module: AdvancedTransfer.Station 3 (Dock Door Station
3)
;
21$      STATION,      Dock Door 3;
372$     DELAY:        0.0,,VA:NEXT(22$);
;
;
;

```

```

; Model statements for module: AdvancedTransfer.Leave 3 (Move to Staging Area
3)
;
22$ DELAY: 0.00,,VA:NEXT(386$);
386$ QUEUE, Move to Staging Area 3.Queue;
390$ REQUEST, 1:Forklift Inbound 3(CYC);
378$ DELAY: 0.0000000000000000,,VA:NEXT(380$);
380$ TRANSPORT: ,Enter Staging Area 3.Station;
;
;
; Model statements for module: AdvancedTransfer.Enter 3 (Enter Staging Area 3)
;
23$ STATION, Enter Staging Area 3.Station;
393$ DELAY: 0.5,,VA:NEXT(395$);
395$ FREE: Forklift Inbound 3:NEXT(50$);
;
;
; Model statements for module: AdvancedProcess.Delay 3 (Process Staging
Product at Staging Area 3)
;
50$ DELAY: EXPO( 0.5 ),,Other:NEXT(51$);
;
;
; Model statements for module: AdvancedTransfer.Enter 4 (Enter Shipping
Station 4)
;
35$ STATION, Enter Shipping Station 4.Station;
404$ DELAY: 0.5,,VA:NEXT(406$);
;
406$ FREE: Forklift Outbound 1:NEXT(25$);
;
;
; Model statements for module: AdvancedProcess.Hold 5 (Hold Until Outbound
Truck 4 Available)
;
25$ QUEUE, Hold Until Outbound Truck 4 Available.Queue;
WAIT: 4,UNIF ( 10,22 ):NEXT(52$);
;
;
; Model statements for module: AdvancedProcess.ReadWrite 5 (ReadWrite 5)
;
52$ WRITE, Total time Product,RECORDSET(Total Time P1):
TNOW-Arrtime P1:NEXT(24$);
;
;
; Model statements for module: BasicProcess.Dispose 2 (Dispose 2)
;
24$ ASSIGN: Dispose 2.NumberOut=Dispose 2.NumberOut + 1;
415$ DISPOSE: Yes;
;
;
; Model statements for module: AdvancedTransfer.Enter 5 (Enter Shipping
Station 5)
;
37$ STATION, Enter Shipping Station 5.Station;
416$ DELAY: 0.5,,VA:NEXT(418$);
;
418$ FREE: Forklift Outbound 2:NEXT(27$);
;
;
; Model statements for module: AdvancedProcess.Hold 6 (Hold Until Outbound
Truck 5 Available)
;
27$ QUEUE, Hold Until Outbound Truck 5 Available.Queue;
WAIT: 5,UNIF ( 10,22 ):NEXT(56$);
;

```

```

;
; Model statements for module: AdvancedProcess.ReadWrite 6 (ReadWrite 6)
;
56$ WRITE, Total time Product,RECORDSET(Total Time P2):
TNOW-Arrtime P2:NEXT(24$);
;
;
; Model statements for module: AdvancedTransfer.Enter 6 (Enter Shipping
Station 6)
;
39$ STATION, Enter Shipping Station 6.Station;
427$ DELAY: 0.5,,VA:NEXT(429$);
429$ FREE: Forklift Outbound 3:NEXT(29$);
;
;
; Model statements for module: AdvancedProcess.Hold 7 (Hold Until Outbound
Truck 6 Available)
;
29$ QUEUE, Hold Until Outbound Truck 6 Available.Queue;
WAIT: 6,UNIF ( 10,22 ):NEXT(57$);
;
;
; Model statements for module: AdvancedProcess.ReadWrite 7 (ReadWrite 7)
;
57$ WRITE, Total time Product,RECORDSET(Total Time P3):
TNOW-Arrtime P3:NEXT(24$);
;
;
; Model statements for module: BasicProcess.Create 5 (Truck Outbound Arrival)
;
438$ CREATE,
1,HoursToBaseTime(2),Truck:HoursToBaseTime(EXPO(1.5)):NEXT(439$);
439$ ASSIGN: Truck Outbound Arrival.NumberOut=Truck Outbound
Arrival.NumberOut + 1:NEXT(44$);
;
;
; Model statements for module: BasicProcess.Decide 4 (Equal Probability
Outbound Truck)
;
44$ BRANCH, 1:
With, (33)/100,40$,Yes:
With, (33)/100,41$,Yes:
Else,42$,Yes;
;
;
; Model statements for module: BasicProcess.Process 9 (Process Load at Dock 6)
;
42$ ASSIGN: Process Load at Dock 6.NumberIn=Process Load at Dock
6.NumberIn + 1:
Process Load at Dock 6.WIP=Process Load at Dock
6.WIP+1;
447$ QUEUE, Process Load at Dock 6.Queue;
446$ SEIZE, 2,VA:
Outbound Dock Door 6,1:NEXT(445$);
;
445$ DELAY: HoursToBaseTime(Triangular(.5,1,1.5)),,VA;
444$ RELEASE: Outbound Dock Door 6,1;
492$ ASSIGN: Process Load at Dock 6.NumberOut=Process Load at Dock
6.NumberOut + 1:
Process Load at Dock 6.WIP=Process Load at Dock 6.WIP-
1:NEXT(47$);
;
;
; Model statements for module: AdvancedProcess.Signal 7 (Signal Discharge 6)
;

```



```

47$          SIGNAL:          6:NEXT(43$);
;
;
;      Model statements for module:  BasicProcess.Dispose 5 (Dispose Outbound)
;
43$          ASSIGN:          Dispose Outbound.NumberOut=Dispose Outbound.NumberOut
+ 1;
495$         DISPOSE:         Yes;
;
;
;      Model statements for module:  BasicProcess.Process 7 (Process Load at Dock 4)
;
40$          ASSIGN:          Process Load at Dock 4.NumberIn=Process Load at Dock
4.NumberIn + 1:
                                     Process Load at Dock 4.WIP=Process Load at Dock
4.WIP+1;
499$         QUEUE,          Process Load at Dock 4.Queue;
498$         SEIZE,          2,VA:
                                     Outbound Dock Door 4,1:NEXT(497$);

497$         DELAY:          HoursToBaseTime(Triangular(.5,1,1.5)),,VA;
496$         RELEASE:        Outbound Dock Door 4,1;
544$         ASSIGN:          Process Load at Dock 4.NumberOut=Process Load at Dock
4.NumberOut + 1:
                                     Process Load at Dock 4.WIP=Process Load at Dock 4.WIP-
1:NEXT(45$);
;
;
;      Model statements for module:  AdvancedProcess.Signal 5 (Signal Discharge 4)
;
45$          SIGNAL:          4:NEXT(43$);

;
;
;      Model statements for module:  BasicProcess.Process 8 (Process Load at Dock 5)
;
41$          ASSIGN:          Process Load at Dock 5.NumberIn=Process Load at Dock
5.NumberIn + 1:
                                     Process Load at Dock 5.WIP=Process Load at Dock
5.WIP+1;
550$         QUEUE,          Process Load at Dock 5.Queue;
549$         SEIZE,          2,VA:
                                     Outbound Dock Door 5,1:NEXT(548$);

548$         DELAY:          HoursToBaseTime(Triangular(.5,1,1.5)),,VA;
547$         RELEASE:        Outbound Dock Door 5,1;
595$         ASSIGN:          Process Load at Dock 5.NumberOut=Process Load at Dock
5.NumberOut + 1:
                                     Process Load at Dock 5.WIP=Process Load at Dock 5.WIP-
1:NEXT(46$);
;
;
;      Model statements for module:  AdvancedProcess.Signal 6 (Signal Discharge 5)
;
46$          SIGNAL:          5:NEXT(43$);

```

Appendix 2

II. Uniform Distribution

Distribution Summary

Distribution: Uniform
 Expression: UNIF(9.5, 22.5)
 Square Error: 0.056213
 Chi Square Test
 Number of intervals = 4
 Degrees of freedom = 3
 Test Statistic = 4.63
 Corresponding p-value = 0.214

Data Summary

Number of Data Points = 26
 Min Data Value = 10
 Max Data Value = 22
 Sample Mean = 16.5
 Sample Std Dev = 4.75

Histogram Summary

Histogram Range = 9,5 to 22.5 (10,22)
 Number of Intervals = 13

Int. No.	No. of Data Pts.	x	Probability Density		Cumulative Distribution	
			Data	Function	Data	Function
0	6	10.0	0.231	0.0769	0.231	0.0769
1	1	11.0	0.0385	0.0769	0.269	0.154
2	1	12.0	0.0385	0.0769	0.308	0.231
3	1	13.0	0.0385	0.0769	0.346	0.308
4	1	14.0	0.0385	0.0769	0.385	0.385
5	0	15.0	0.000	0.0769	0.385	0.462
6	1	16.0	0.0385	0.0769	0.423	0.538
7	1	17.0	0.0385	0.0769	0.462	0.615
8	3	18.0	0.115	0.0769	0.577	0.692
9	1	19.0	0.0385	0.0769	0.615	0.769
10	3	20.0	0.115	0.0769	0.731	0.846
11	2	21.0	0.0769	0.0769	0.808	0.923
12	5	22.0	0.192	0.0769	1.00	1.00

Appendix 3

Half Width Table

degrees of freedom	1 - $\alpha/2$				
	0.900	0.950	0.975	0.990	0.995
1	3.078	6.314	12.706	31.821	63.656
2	1.886	2.920	4.303	6.965	9.925
3	1.638	2.353	3.182	4.541	5.841
4	1.533	2.132	2.776	3.747	4.604
5	1.476	2.015	2.571	3.365	4.032
6	1.440	1.943	2.447	3.143	3.707
7	1.415	1.895	2.365	2.998	3.499
8	1.397	1.860	2.306	2.896	3.355
9	1.383	1.833	2.262	2.821	3.250
10	1.372	1.812	2.228	2.764	3.169
11	1.363	1.796	2.201	2.718	3.106
12	1.356	1.782	2.179	2.681	3.055
13	1.350	1.771	2.160	2.650	3.012
14	1.345	1.761	2.145	2.624	2.977
15	1.341	1.763	2.131	2.602	2.947
16	1.336	1.746	2.120	2.583	2.921
17	1.333	1.740	2.110	2.567	2.898
18	1.330	1.734	2.101	2.552	2.878
19	1.328	1.729	2.093	2.539	2.861
20	1.325	1.725	2.086	2.528	2.845
25	1.316	1.708	2.060	2.485	2.787
30	1.310	1.697	2.042	2.457	2.750